



Rapid QSM Acquisition with Wave-CAIPI

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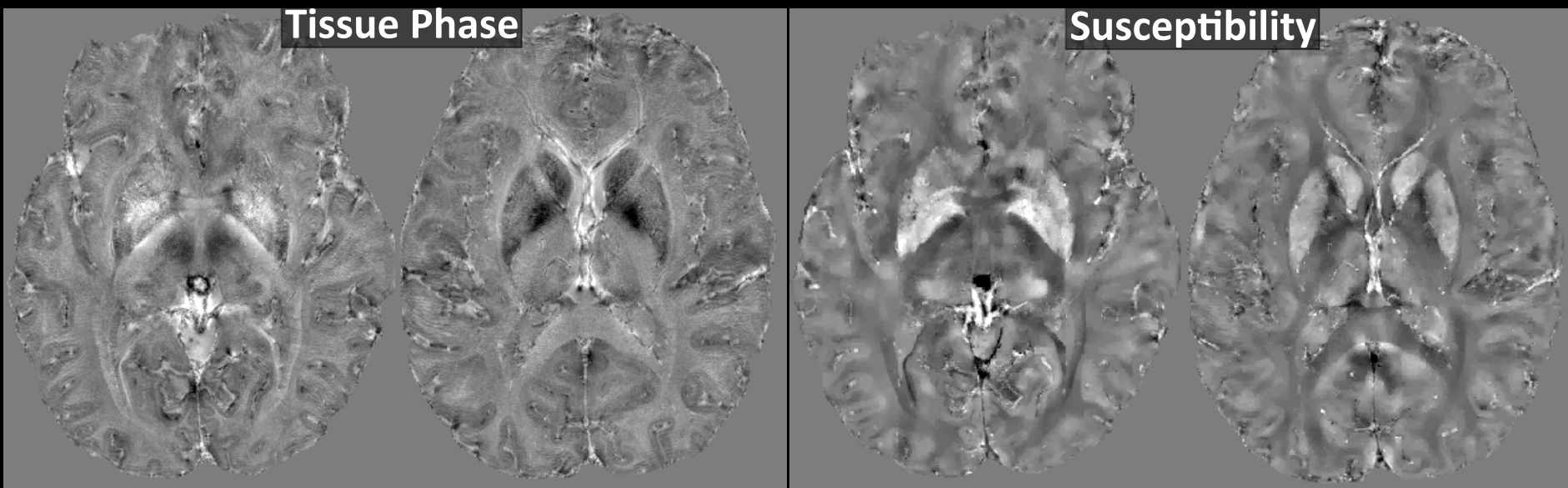
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4 Massachusetts Institute of Technology, Cambridge, MA

5 Harvard-MIT Division of Health Sciences and Technology, Cambridge, MA

Wave-CAIPI accelerated QSM

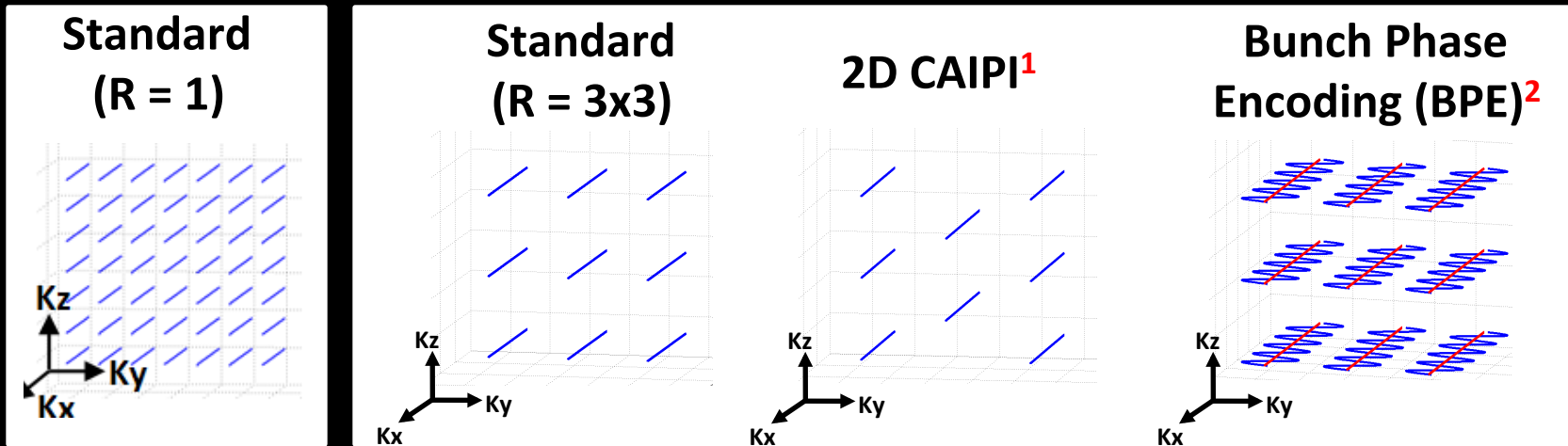
- Quantitative Susceptibility Mapping (QSM) relies on phase data from 3D Gradient Echo (GRE)
- Long echo times ($TE \approx 30\text{ms}$) are required for phase contrast \rightarrow **TR $\geq 30\text{ms}$ very long scan time**



0.5 mm isotropic whole brain @ 7T in 5 minutes
Wave-CAIPI with 9-fold acceleration ($TE/TR=20/30$ ms)

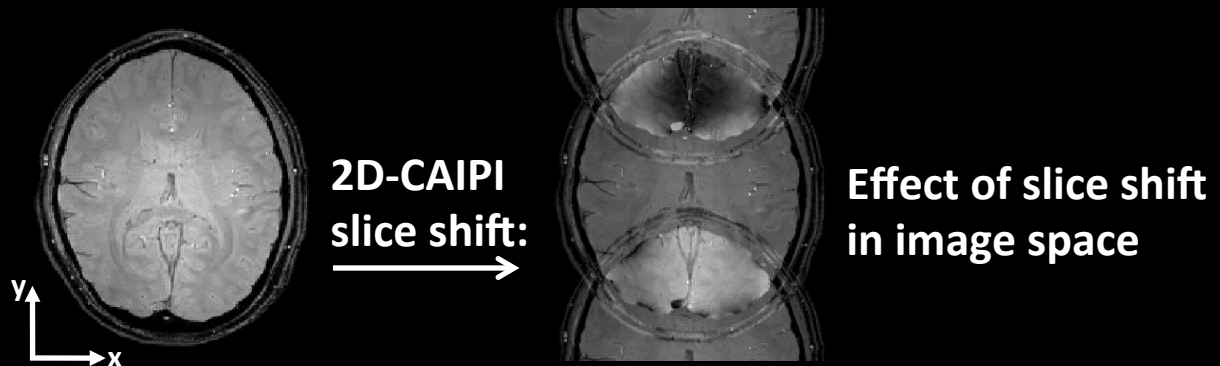
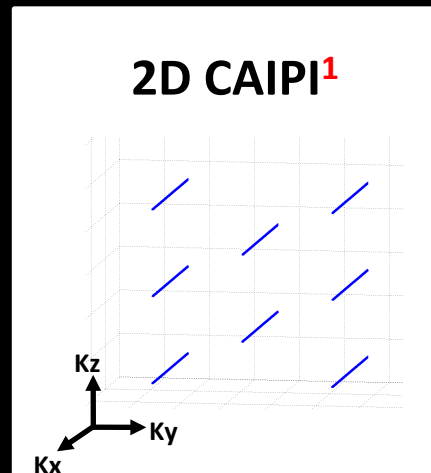
Highly Accelerated 3D Cartesian Imaging

- Recent modifications to rectilinear k-space sampling provided more robust reconstructions of highly under-sampled datasets



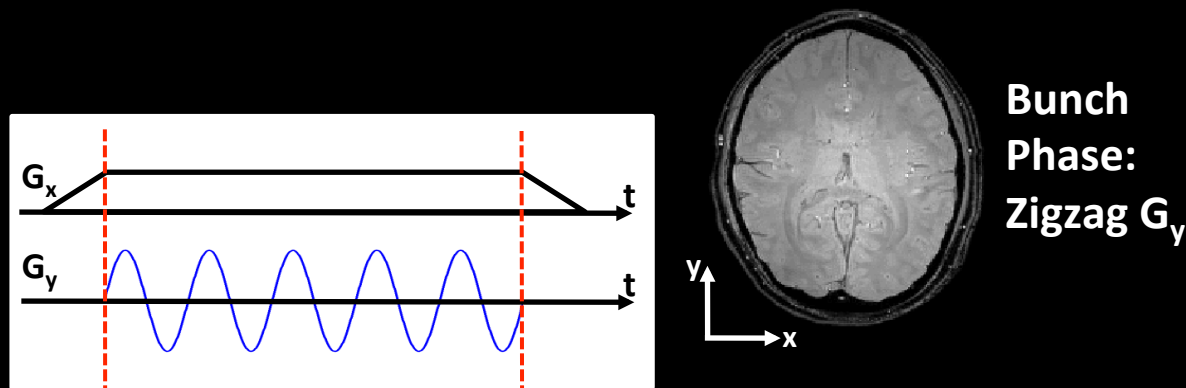
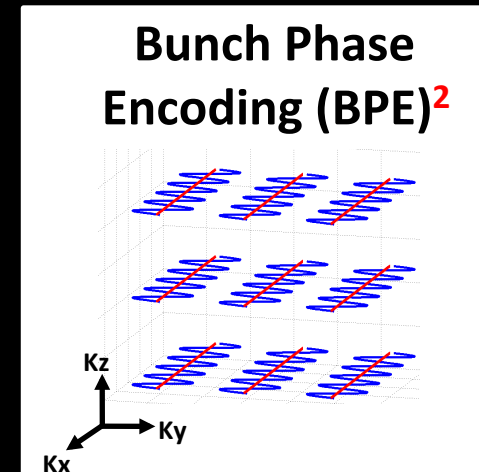
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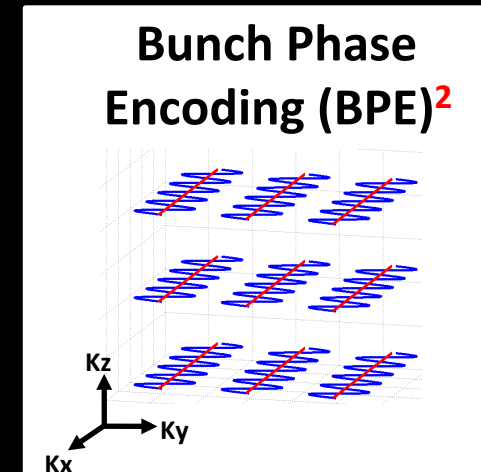
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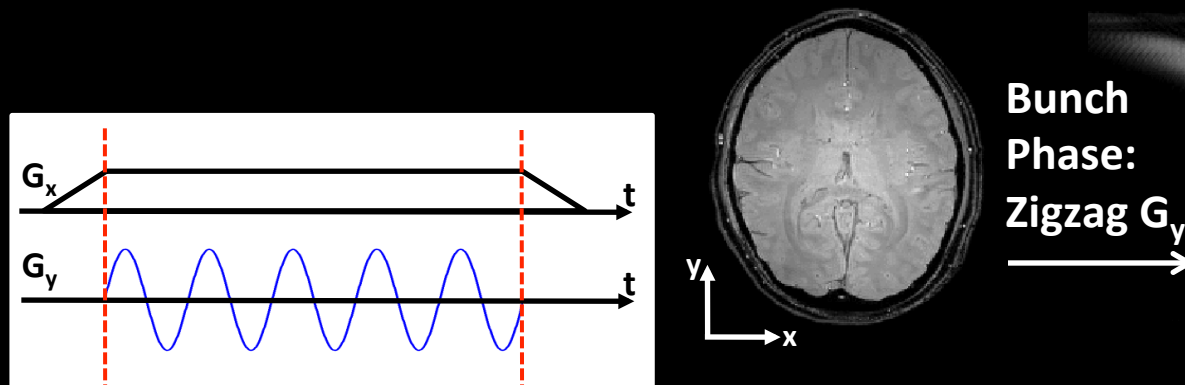


Highly Accelerated 3D Cartesian Imaging

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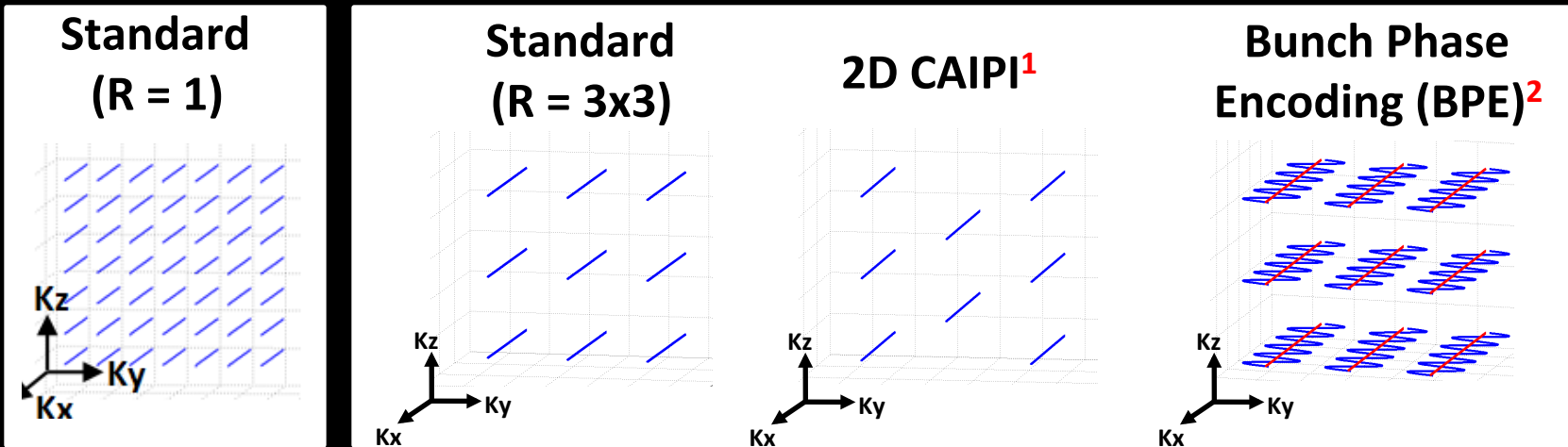


Effect of G_y in image space

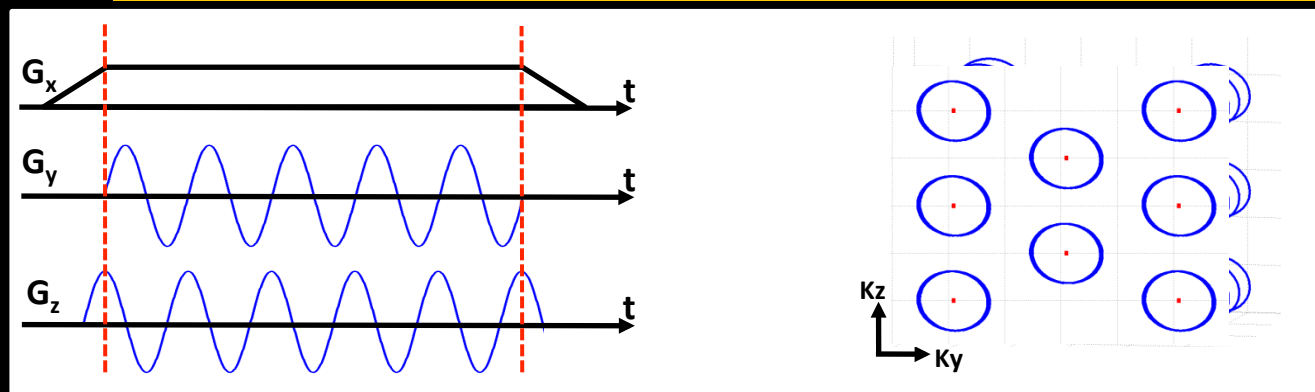


Wave-CAIPI Sampling

- Recent modifications to rectilinear k-space sampling provided more robust reconstructions of highly under-sampled datasets

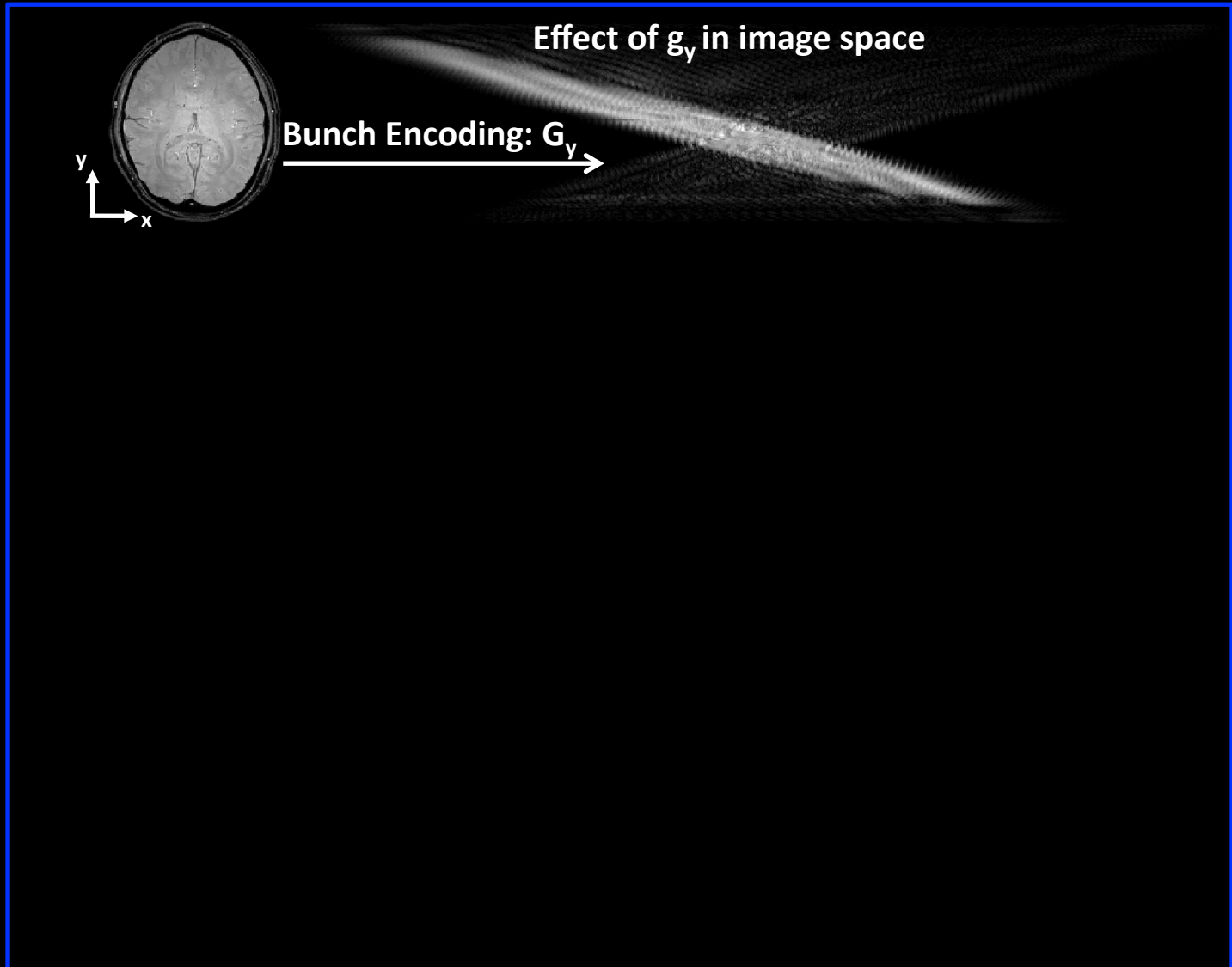


- Wave-CAIPI: 2D CAIPI + BPE in 2 directions
- Spread aliasing in 3D to take full advantage of 3D coil profiles



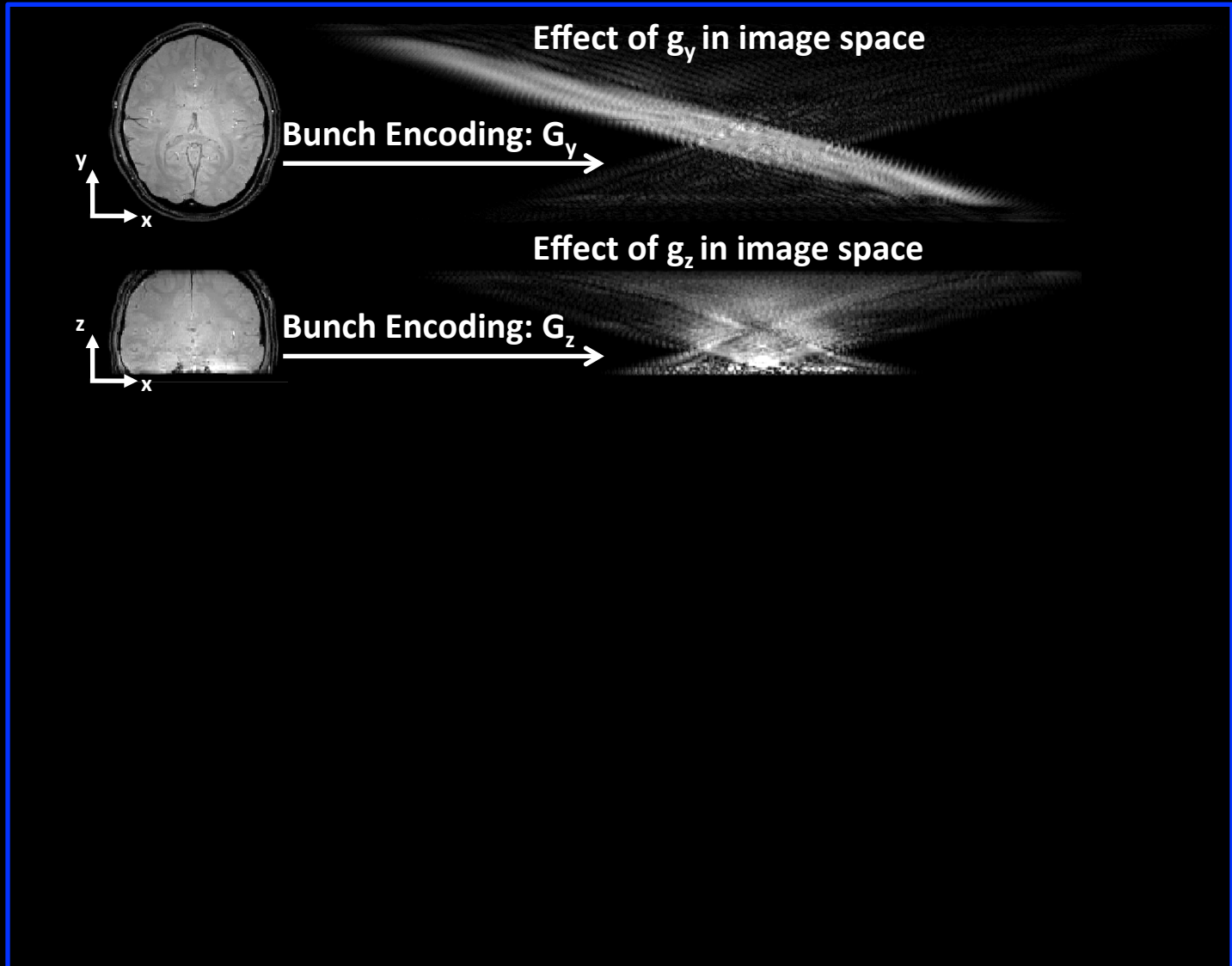
Wave-CAIPI causes voxel spreading in 3 dimensions

- Combination of G_y and G_z gradients with inter-slice shifts yields voxel spreading across three dimensions



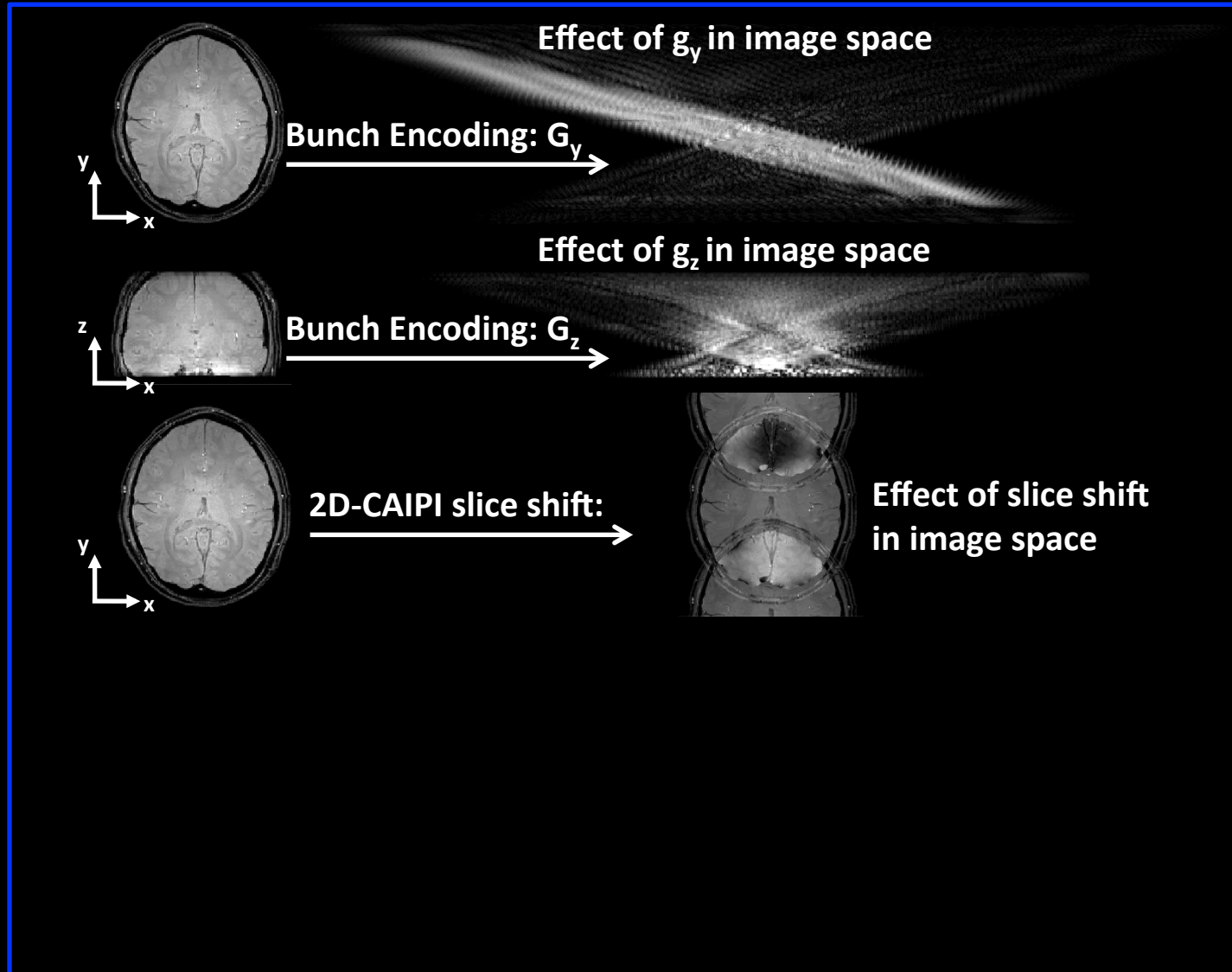
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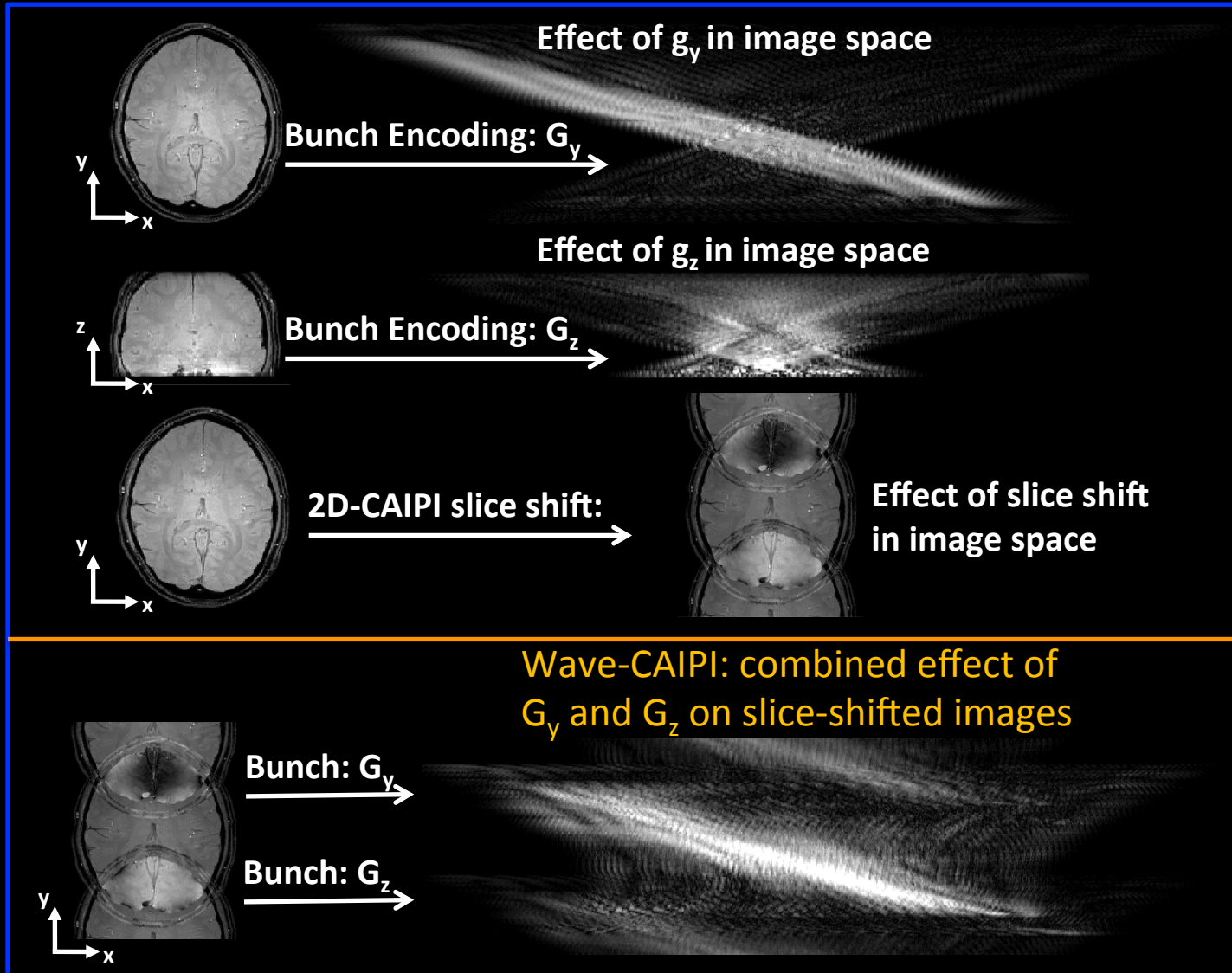
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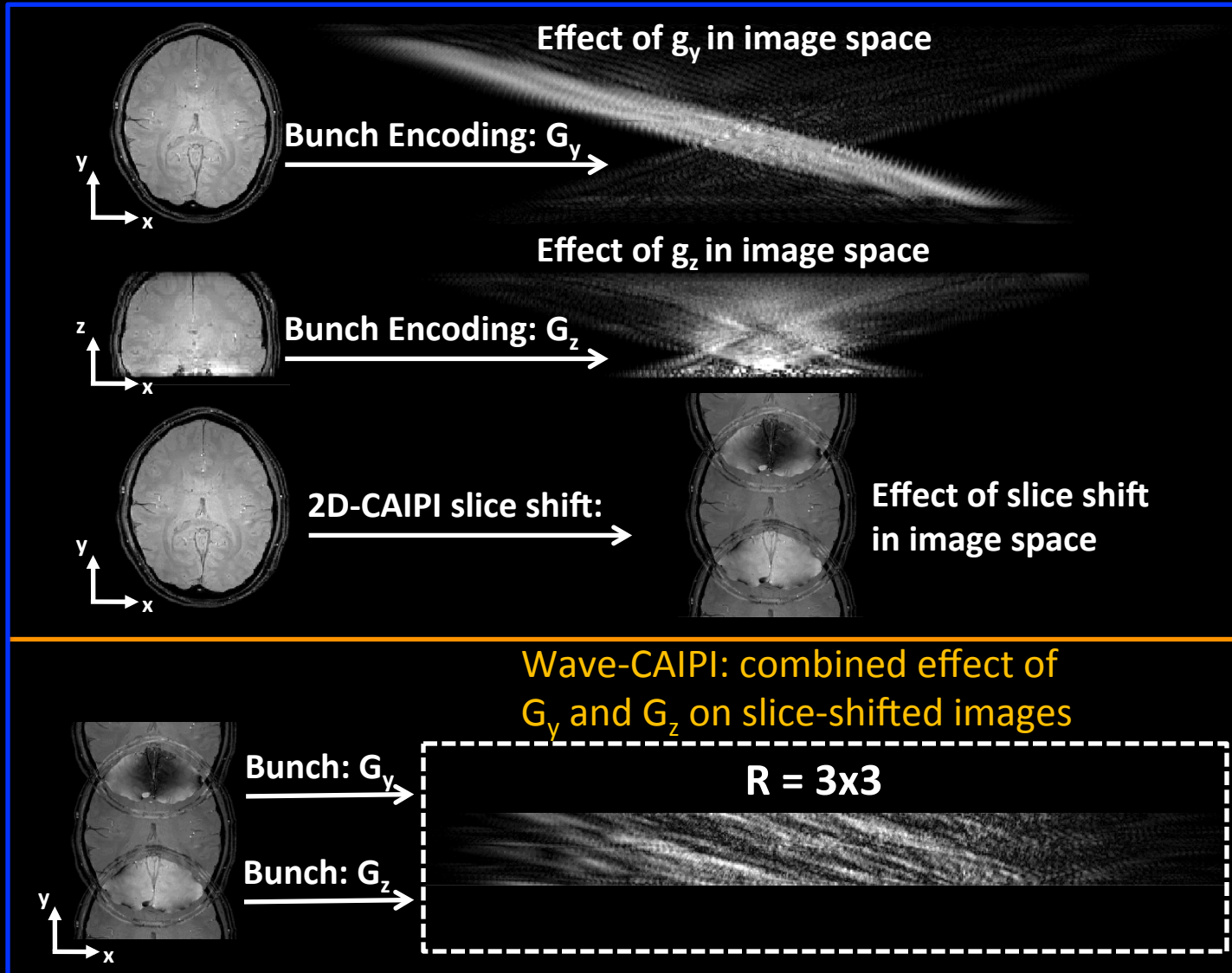
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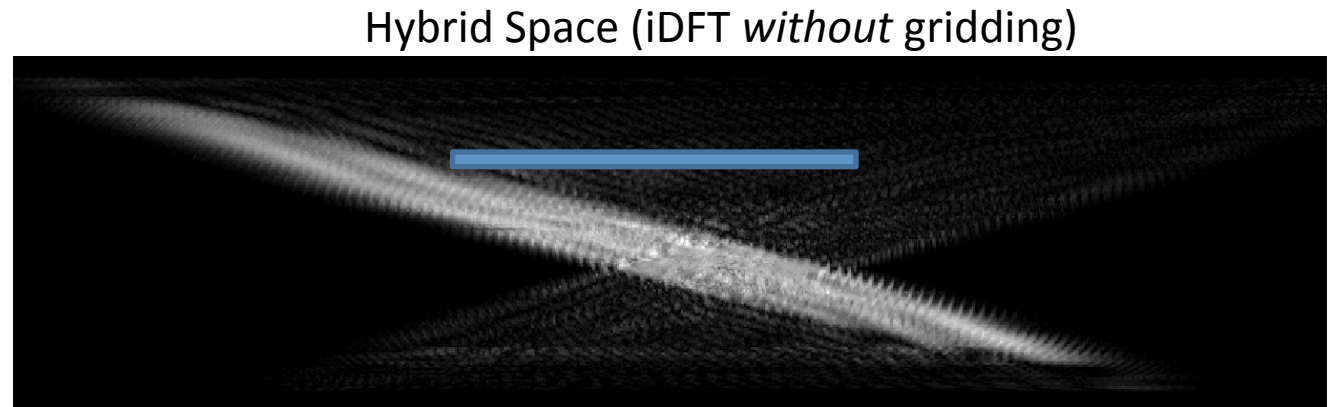
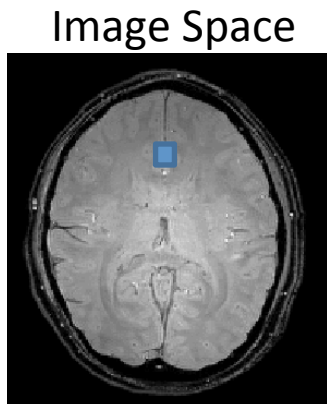
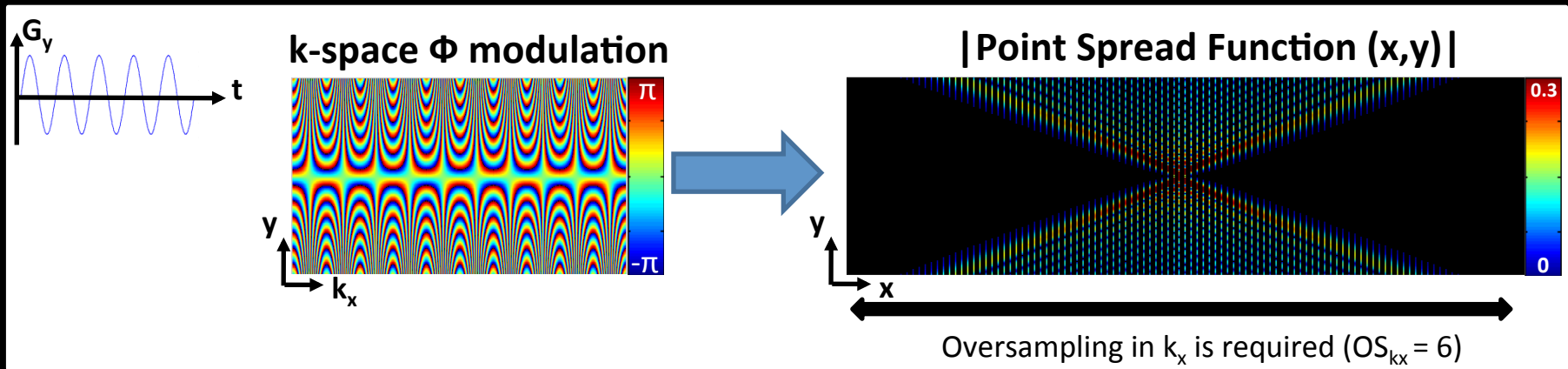
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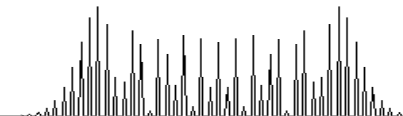


Point Spread Function

- Wave-CAIPI = BPE G_y + BPE G_z + CAIPI 2D
- View BPE G_y as extra modulation rather than modifying k-space traj.



$| \text{PSF}(x,y) |$



Point Spread Function

- From signal equation:

$$wave(x, y, z) = \sum_{k_x} e^{i2\pi x k_x / N} \cdot e^{-i2\pi W_y(k_x) y} \cdot \sum_x e^{-i2\pi x k_x / N} \cdot img(x, y, z)$$

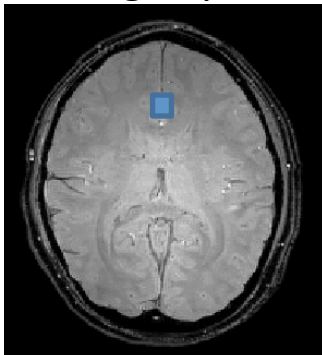
$wave(x, y, z)$ Wave image

$img(x, y, z)$ Underlying magnetization

$$W_y(k_x(t)) = \frac{\gamma}{2\pi} \int_0^t G_y(\tau) d\tau$$

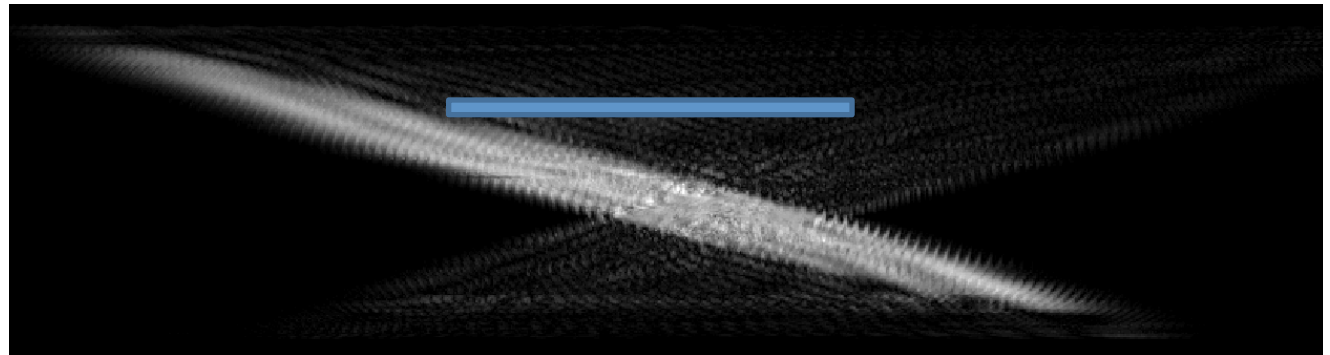
k-space trajectory

Image Space



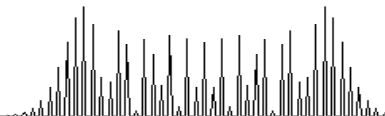
$img(x, y, z)$

Hybrid Space (iDFT *without* gridding)



$|PSF(x, y)|$

$wave(x, y, z)$

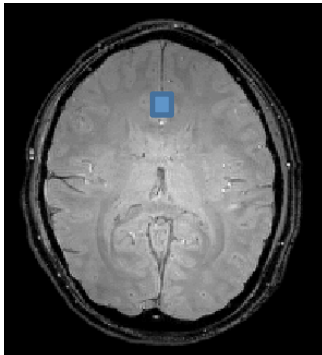


Point Spread Function

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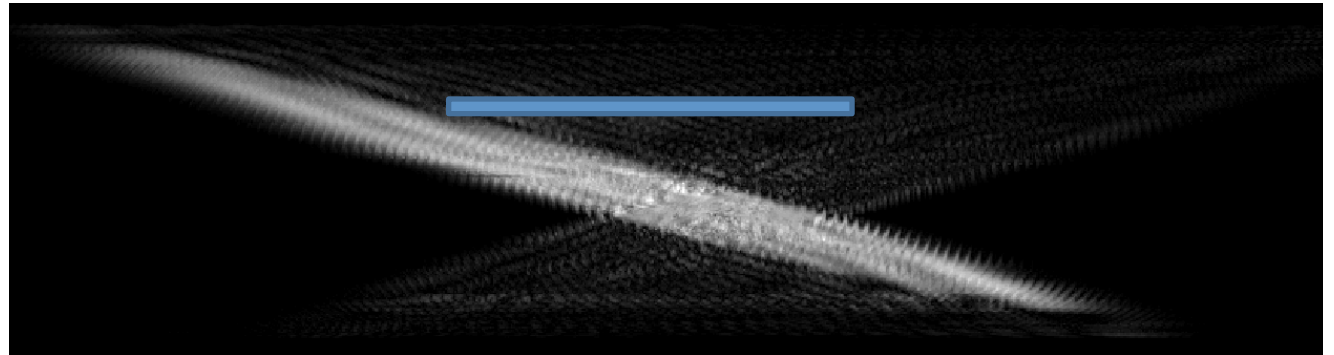
$$wave(x, y, z) = \underbrace{\sum_{k_x} e^{i2\pi x k_x / N}}_{\text{Inverse Discrete Fourier Transform}} \cdot e^{-i2\pi W_y(k_x) y} \cdot \underbrace{\sum_x e^{-i2\pi x k_x / N}}_{\text{Discrete Fourier Transform}} \cdot img(x, y, z)$$

Image Space



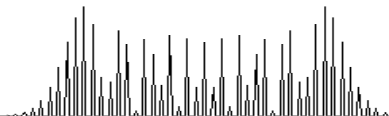
$img(x, y, z)$

Hybrid Space (iDFT *without* gridding)



$|PSF(x, y)|$

$wave(x, y, z)$



Point Spread Function

- From signal equation:

$$wave(x, y, z) = F^{-1} \cdot \underbrace{e^{-i2\pi W_y(k_x)y}}_{\text{Point Spread Function (PSF)}} \cdot F \cdot img(x, y, z)$$

Point Spread Function (PSF)

No need for gridding, simple DFT

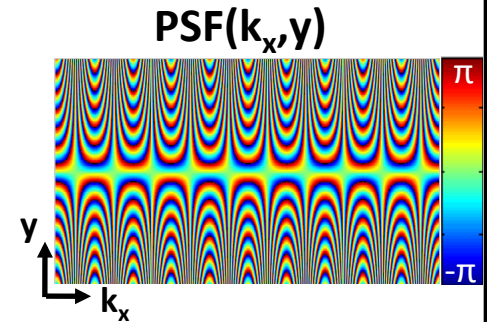
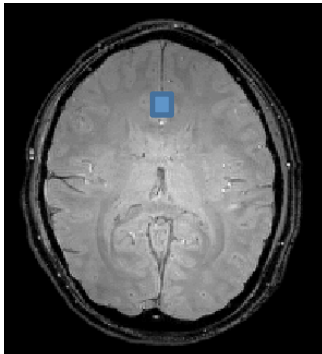
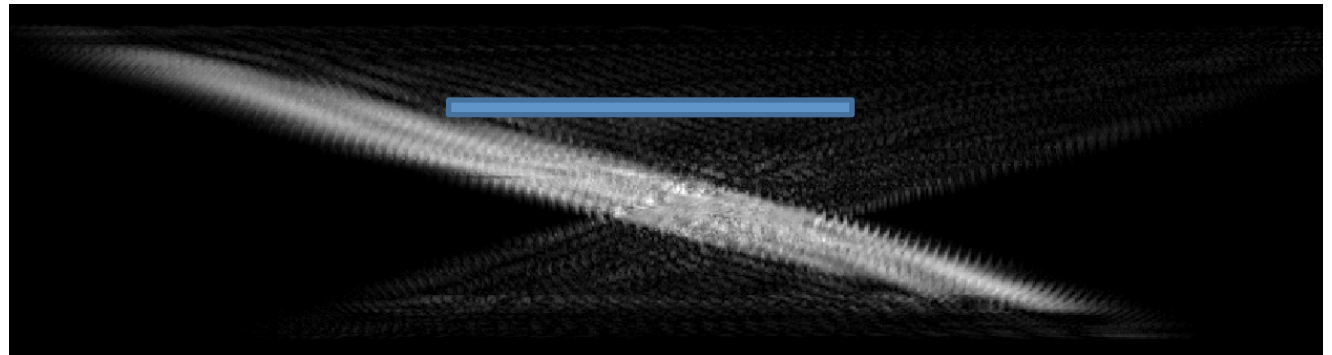


Image Space



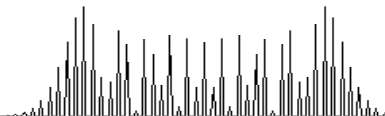
$img(x, y, z)$

Hybrid Space (iDFT *without* gridding)

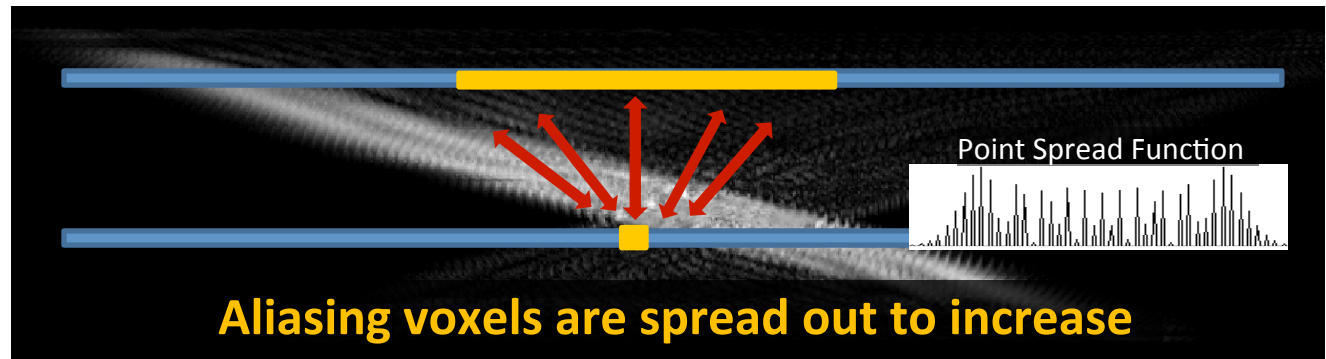
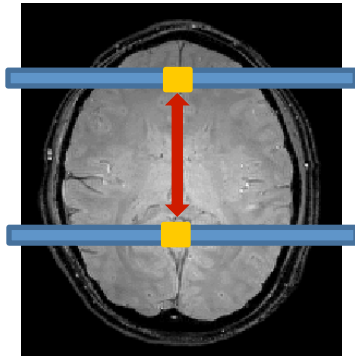


$|PSF(x,y)|$

$wave(x, y, z)$



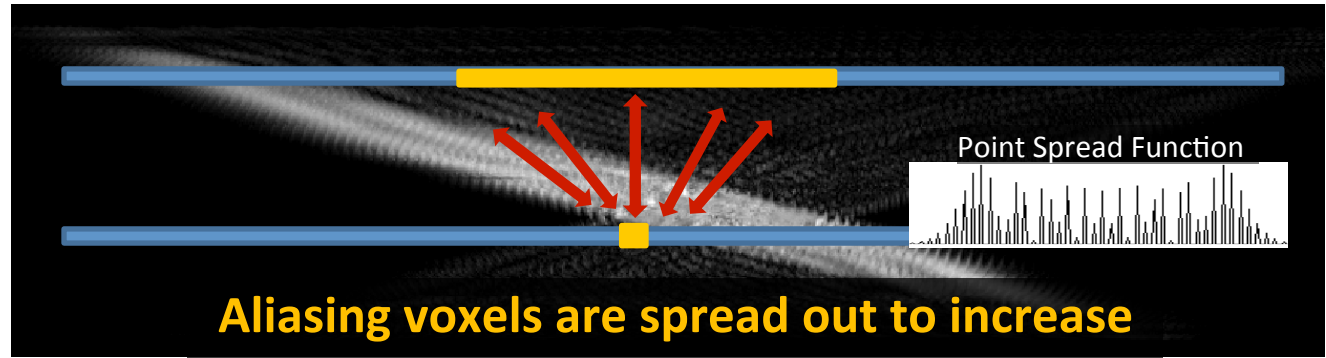
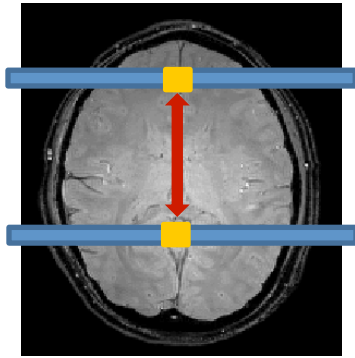
Reconstruction for accelerated acquisitions



Aliasing voxels are spread out to increase the variation in coil sensitivity profiles

- $R_{\text{inplane}} = 2$ => pair-wise aliasing of two rows of voxels
- => small Encoding matrix for each pair
- => separable and easy to solve
- => intuition on why Wave improves reconstruction

Reconstruction for accelerated acquisitions

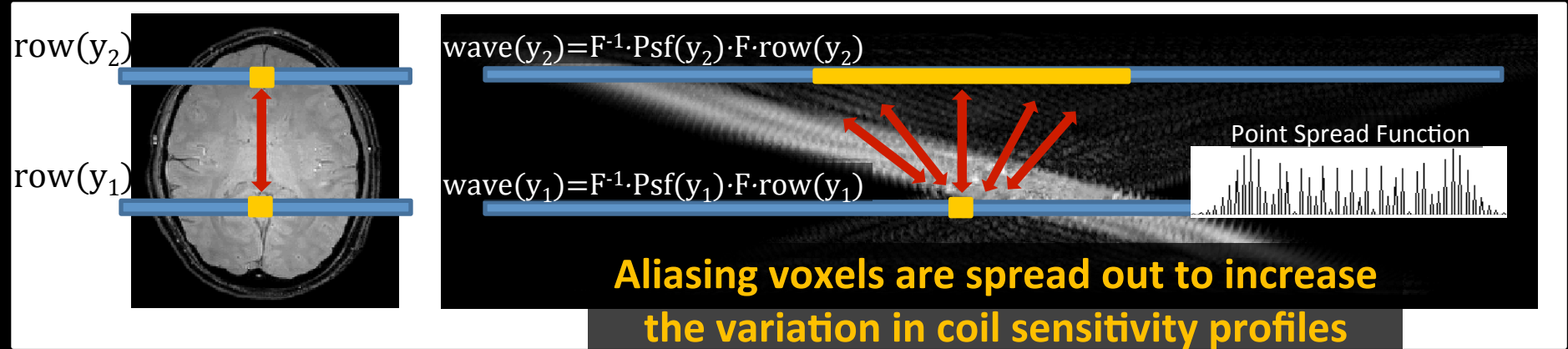


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$$wave(x, y, z) = F^{-1} \cdot \underbrace{e^{-i2\pi W_y(k_x)y}}_{\text{Psf}(y)} \cdot F \cdot img(x, y, z)$$

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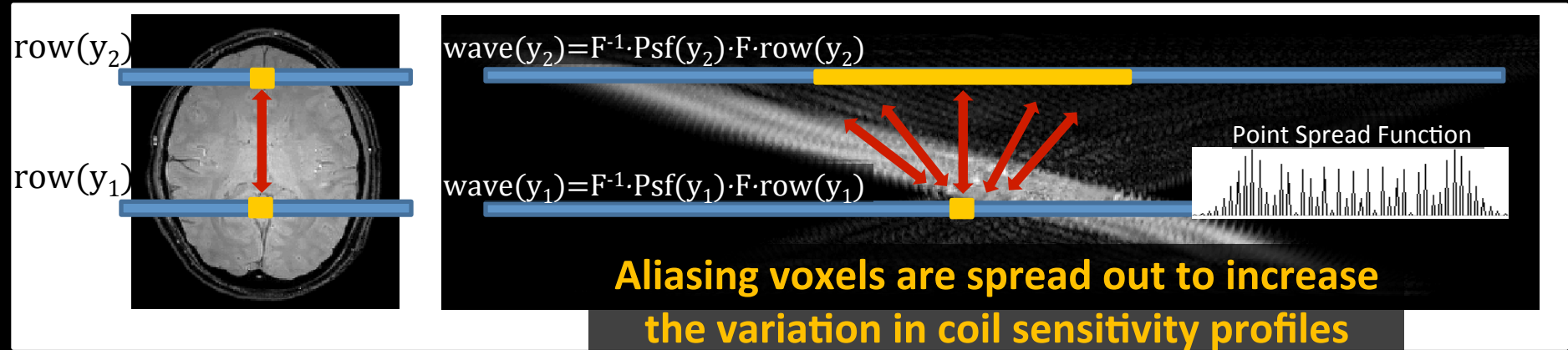


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$$wave(y) = F^{-1} \cdot Psf(y) \cdot F \cdot row(y)$$

$$\begin{bmatrix} F^{-1} \cdot Psf(y_1) \cdot F \\ F^{-1} \cdot Psf(y_2) \cdot F \end{bmatrix} \cdot \begin{bmatrix} row(y_1) \\ row(y_2) \end{bmatrix} = [wave(y_1) + wave(y_2)]$$

Reconstruction for accelerated acquisitions

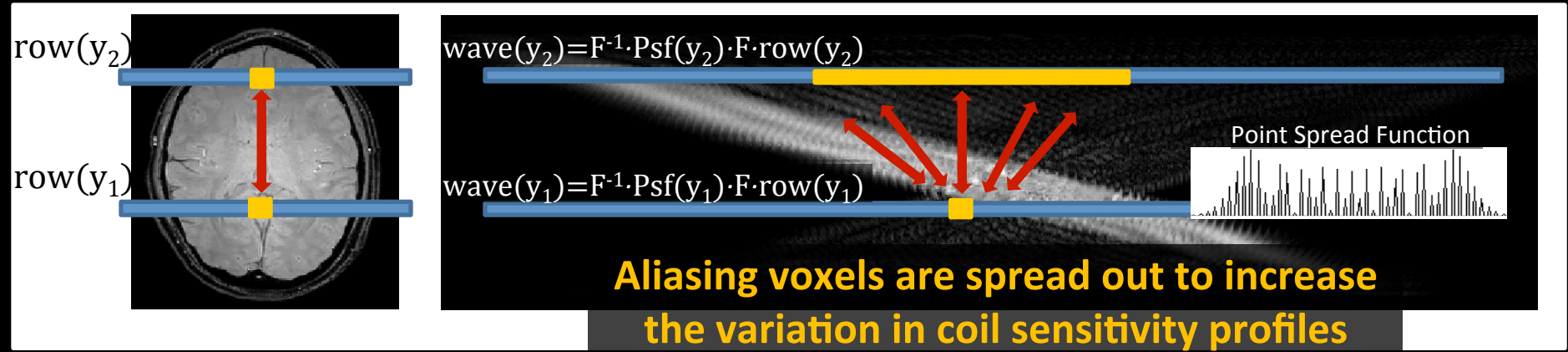


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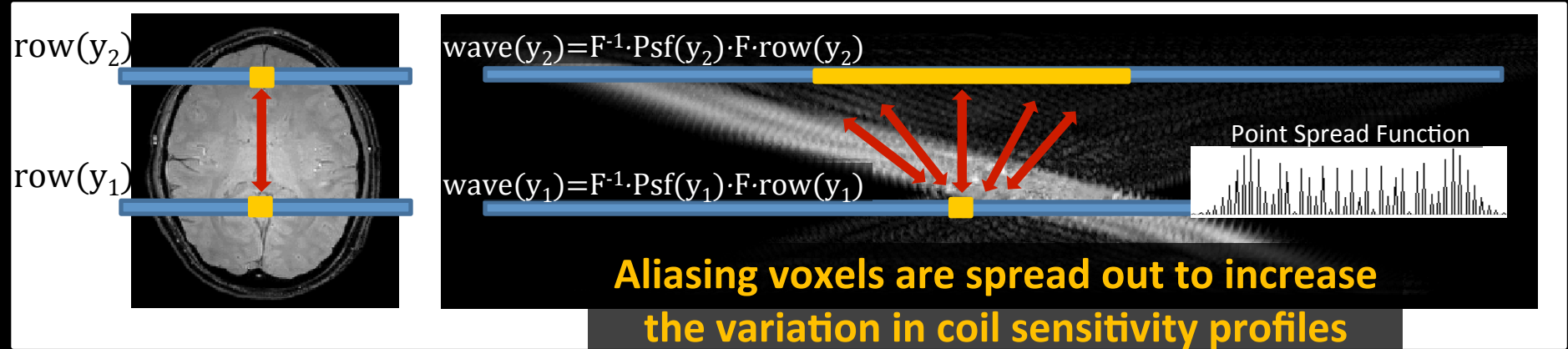


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Reconstruction for accelerated acquisitions



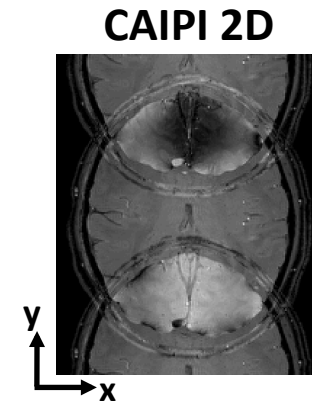
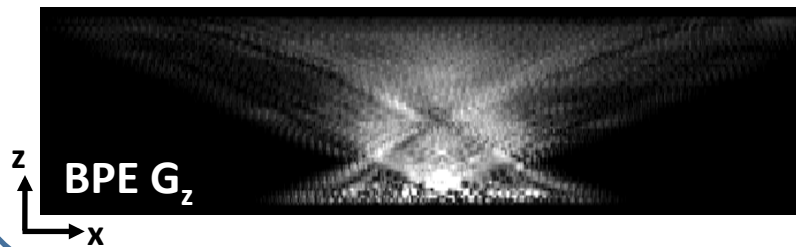
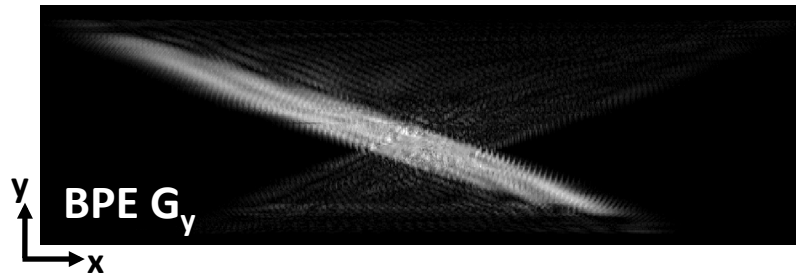
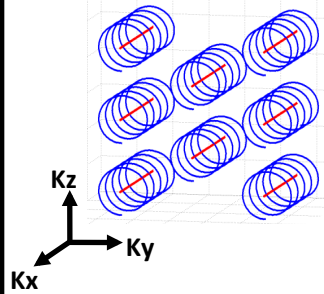
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- Solve for each set of collapsed rows iteratively using LSQR

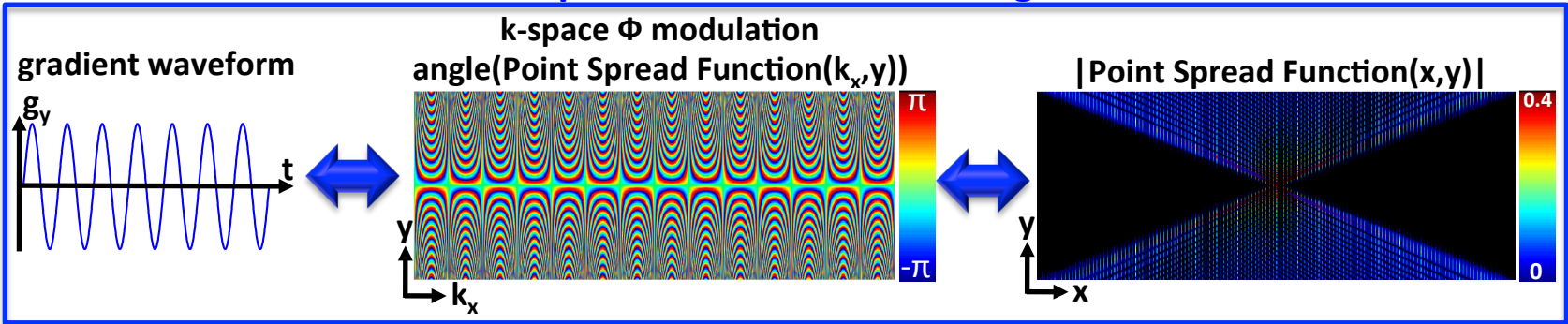
Wave-CAIPI reconstruction



- ⇒ Wave gradients G_y and G_z create position dependent PSF
- ⇒ CAIPI 2D shift aliasing pattern
- ⇒ These are accounted for when generating the PSF-based Encoding matrices
 - ⇒ Ex: $R = 3 \times 3$
 - ⇒ each Encoding matrix corresponds to 9 rows of the image
 - ⇒ grouping of rows is determined by CAIPI 2D
 - ⇒ amount of spreading in each row determined by G_y and G_z

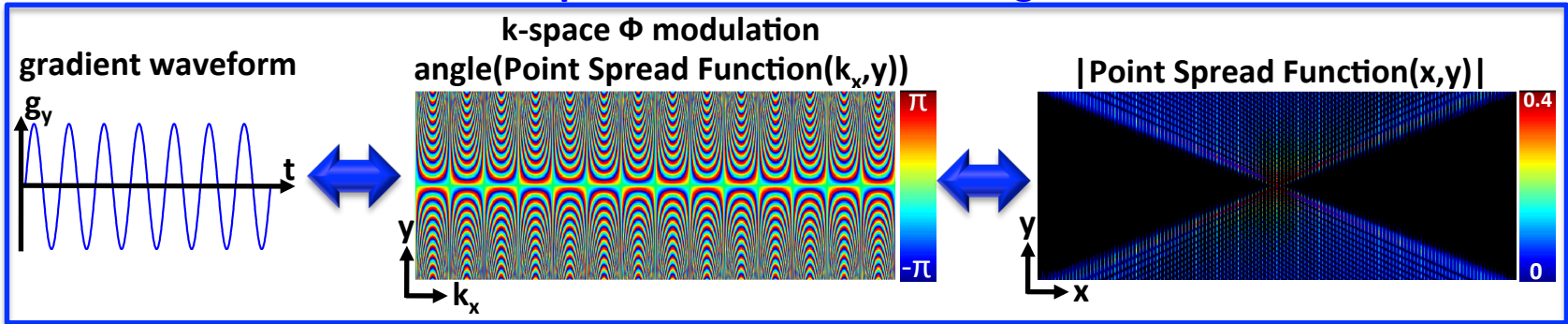
Artifact Quantification

Point Spread Function over image FOV

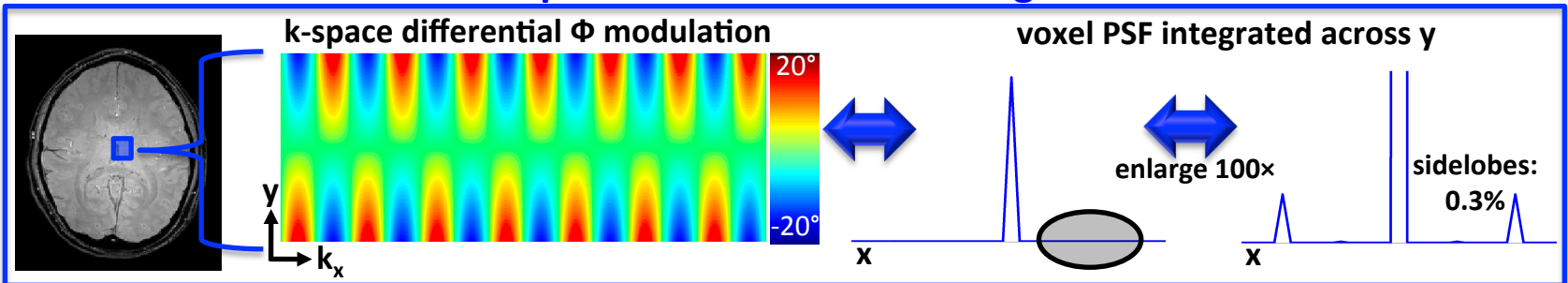


Artifact Quantification

Point Spread Function over image FOV



Point Spread Function within single voxel



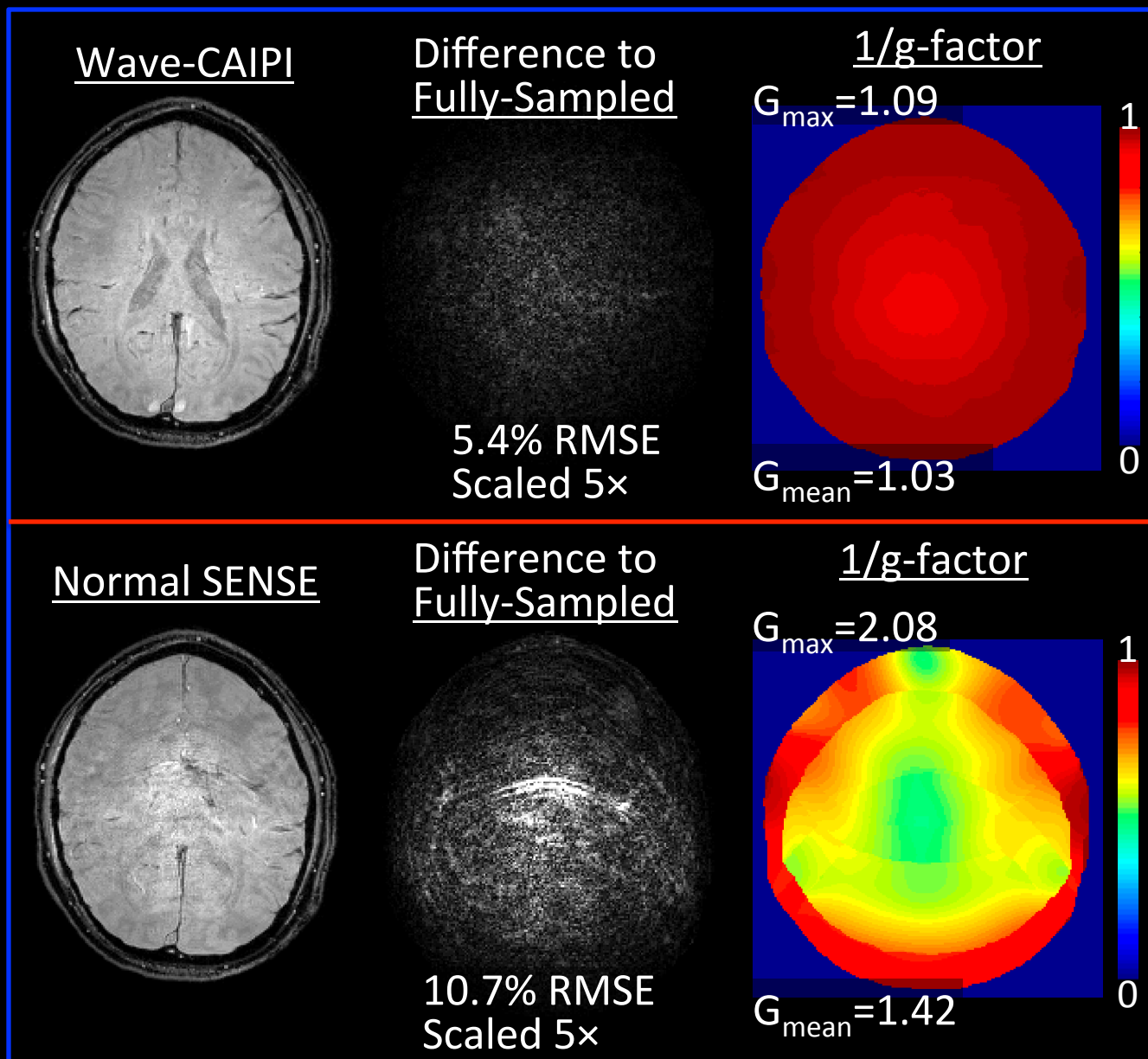
In Vivo Acquisition Comparison

- Compare Wave-CAIPI and conventional SENSE
- Acquire **fully-sampled** data, then accelerate by $R = 3 \times 3$
- Compute root-mean-square error (RMSE) and $1/g$ -factor maps (retained SNR)

In Vivo Acquisition Comparison

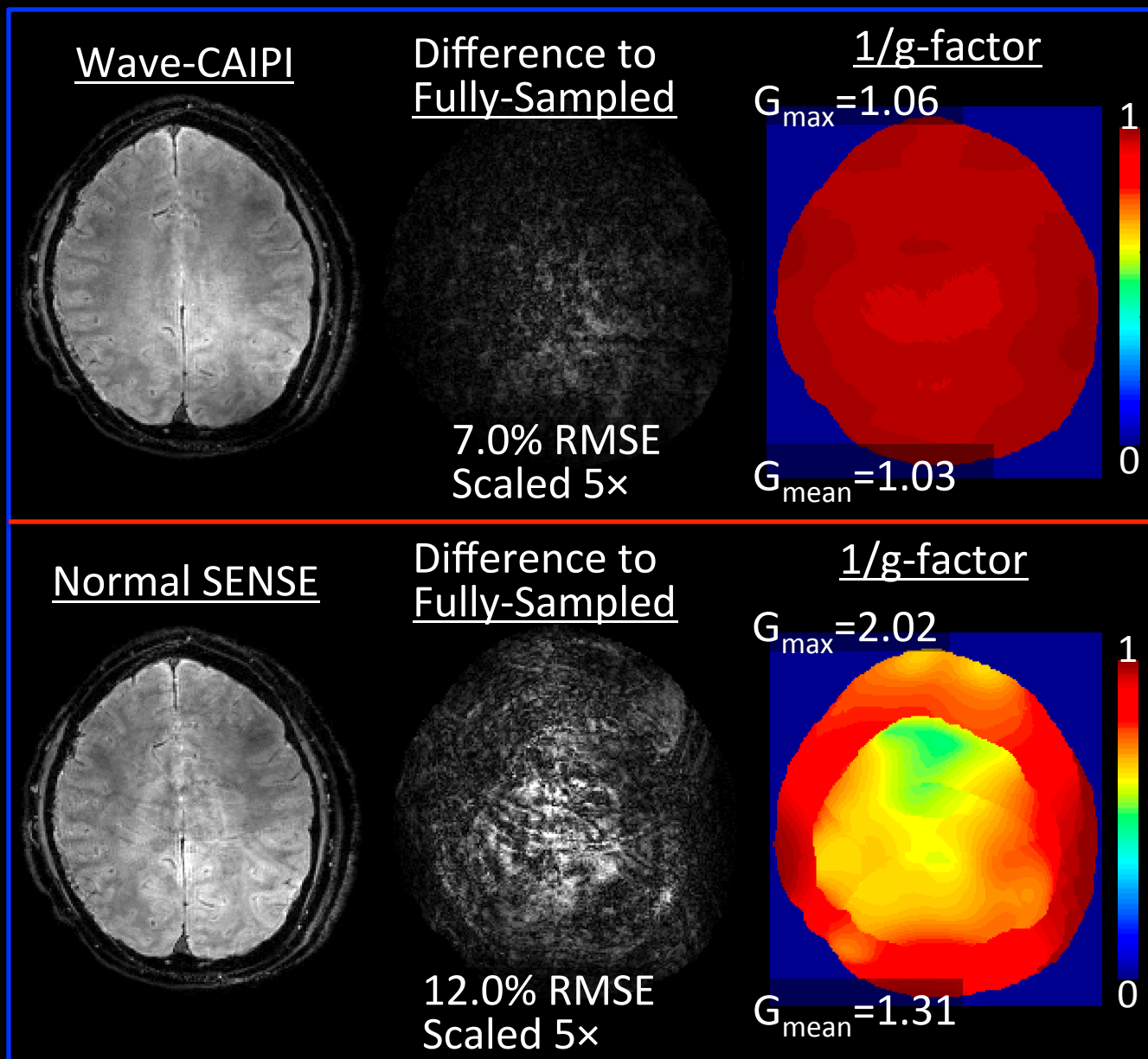
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- Acquire **fully-sampled** data, then accelerate by $R = 3 \times 3$
- Compute root-mean-square error (RMSE) and $1/g$ -factor maps (retained SNR)
- In vivo acquisitions:
 - At 3T and 7T
 - $1 \times 1 \times 2$ mm resolution
 - $224 \times 224 \times 120$ FOV

3 Tesla, R=3x3, 1x1x2 mm³, T_{acq}=38s



TR/TE = 26/13.3 ms

7 Tesla, R=3x3, 1x1x2 mm³, T_{acq}=40s



TR/TE = 27/10.9 ms

Accelerated Acquisition Comparison

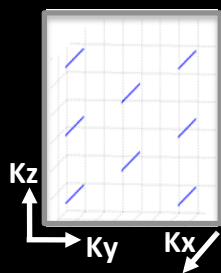
- Compare Wave-CAIPI, 2D-CAIPI¹ and Bunch Phase²
- Acquire R = 3x3 accelerated data
- Compute 1/g-factor maps (retained SNR)

Accelerated Acquisition Comparison

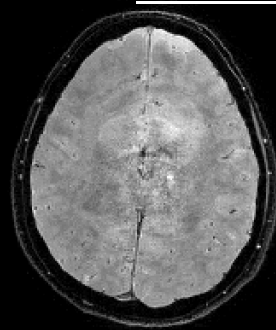
- Compare Wave-CAIPI, 2D-CAIPI¹ and Bunch Phase²
- Acquire R = 3x3 accelerated data
- Compute 1/g-factor maps (retained SNR)
- In vivo acquisitions:
 - At 3T and 7T
 - 1x1x1 mm isotropic resolution
 - Acquisition time: 2.3 min
 - 240x240x120 FOV

R=3x3 @ 3 Tesla, 1 mm iso, $T_{acq}=2.3\text{min}$

k-space

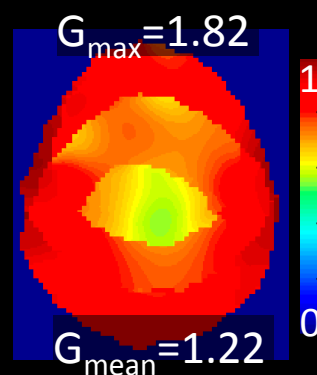


Recon



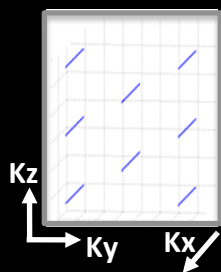
2D-CAIPI

1/G-factor



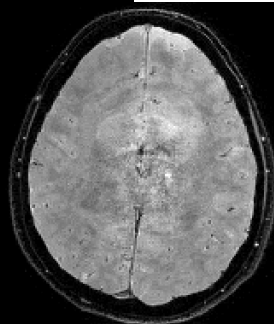
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k-space

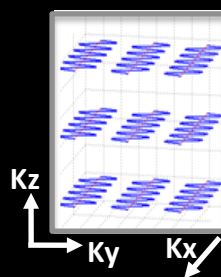
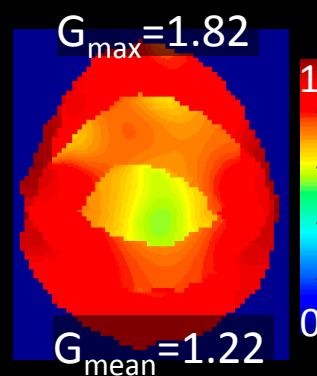


Recon

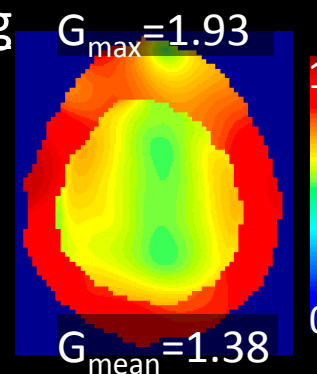
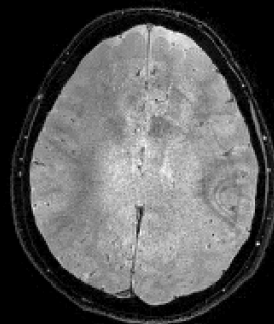
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1/G-factor

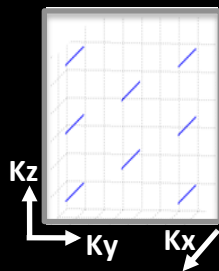


Bunch Encoding

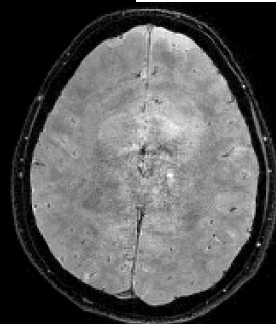


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k-space

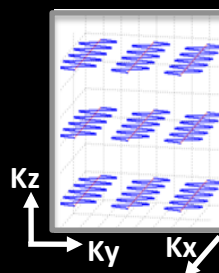
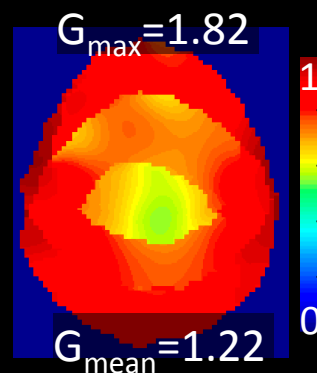


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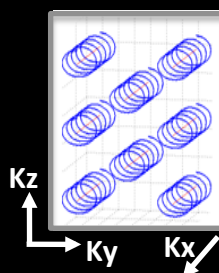
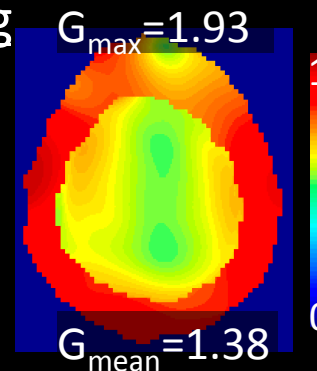
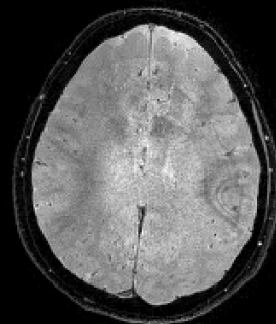


2D-CAPI

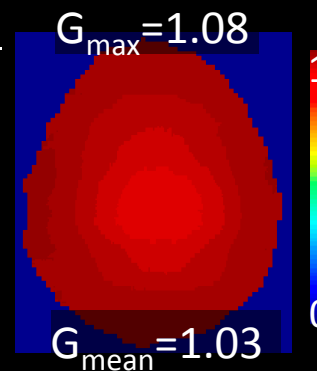
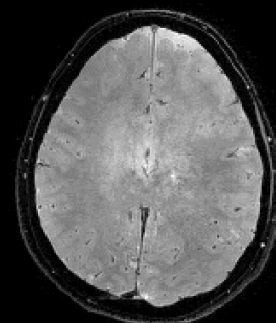
1/G-factor



Bunch Encoding

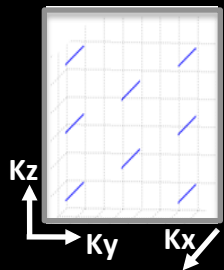


Wave-CAPI

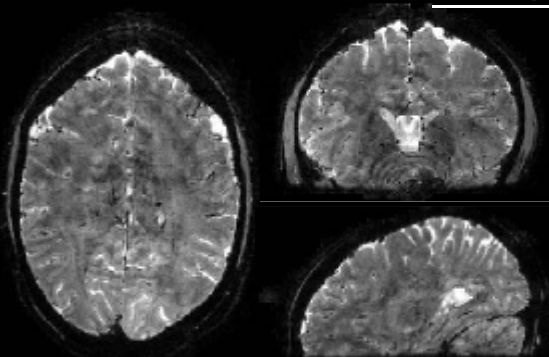


R=3x3 @ 7 Tesla, 1 mm iso, $T_{acq}=2.3\text{min}$

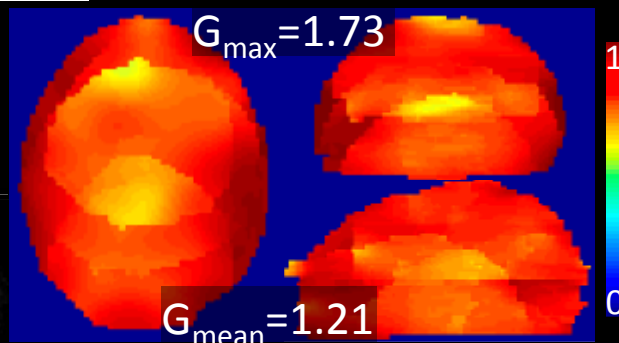
k-space



Recon



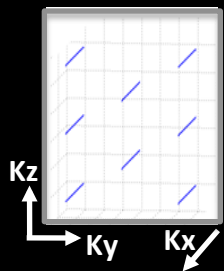
2D-CAIPI



1/G-factor

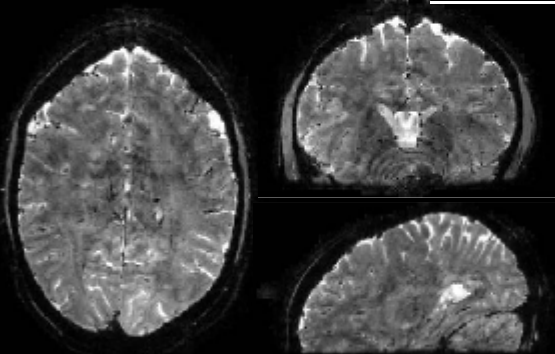
R=3x3 @ 7 Tesla, 1 mm iso, $T_{acq}=2.3\text{min}$

k-space

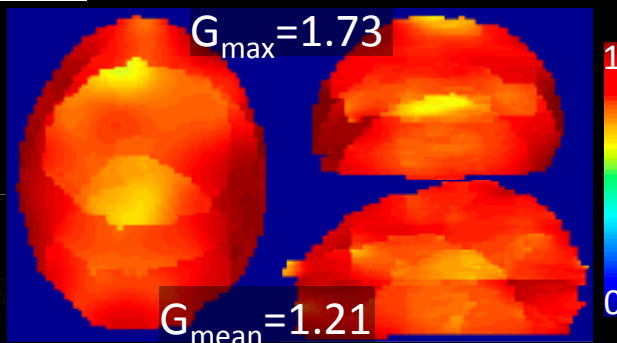


Recon

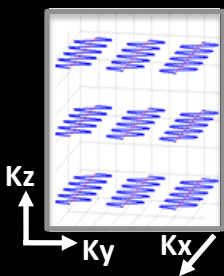
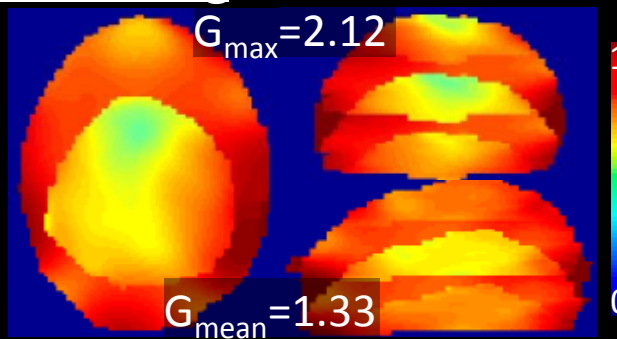
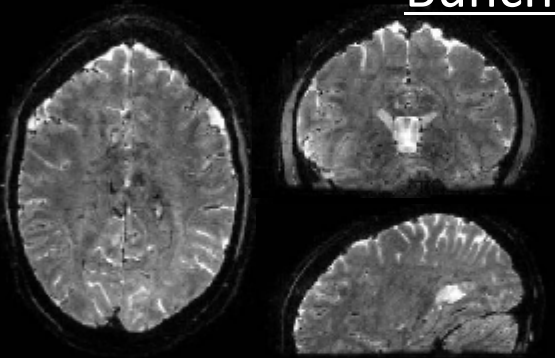
2D-CAIPI



1/G-factor

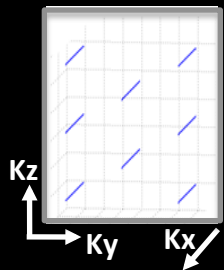


Bunch Encoding



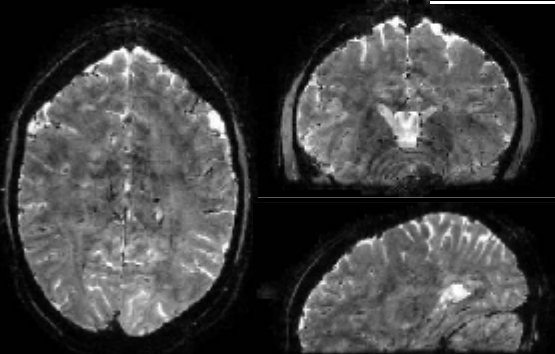
R=3x3 @ 7 Tesla, 1 mm iso, $T_{acq}=2.3\text{min}$

k-space

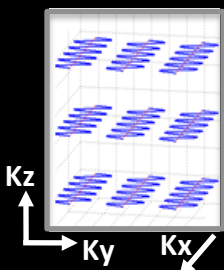
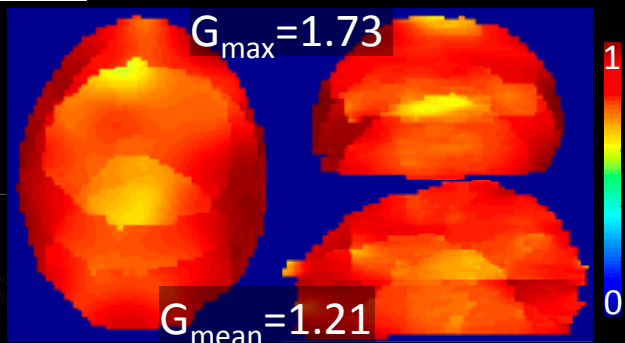


Recon

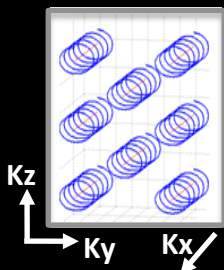
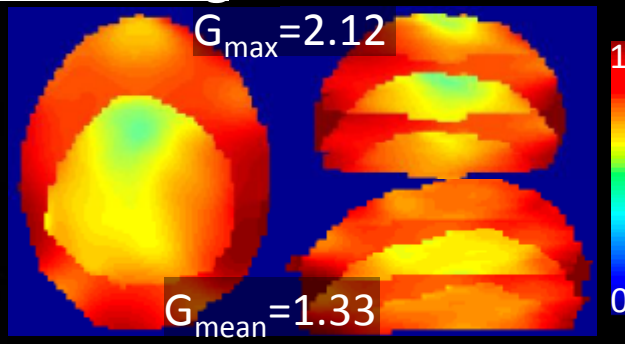
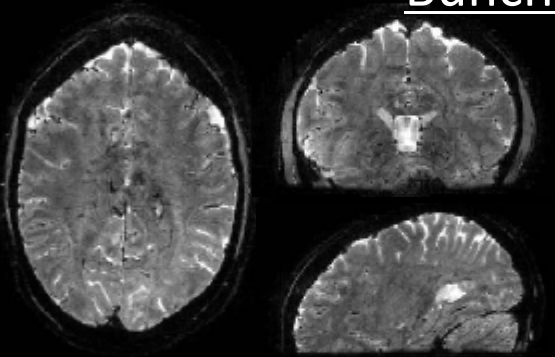
2D-CAIPI



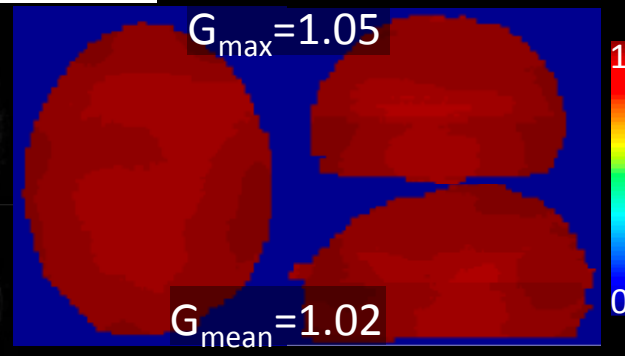
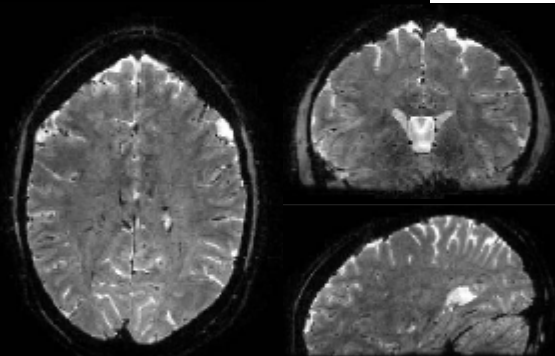
1/G-factor



Bunch Encoding



Wave-CAIPI



Quantitative Susceptibility Mapping (QSM)

- QSM estimates the underlying magnetic susceptibility that gives rise to subtle changes in the magnetic field
- Estimation of the susceptibility map χ from the unwrapped phase φ involves solving an inverse problem¹,

$$\delta = \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \chi$$

measured estimate

\mathbf{F} : Discrete Fourier Transform

\mathbf{D} : susceptibility kernel

$\delta = \varphi / (\gamma \cdot TE \cdot B_0)$: normalized field map

Quantitative Susceptibility Mapping (QSM)

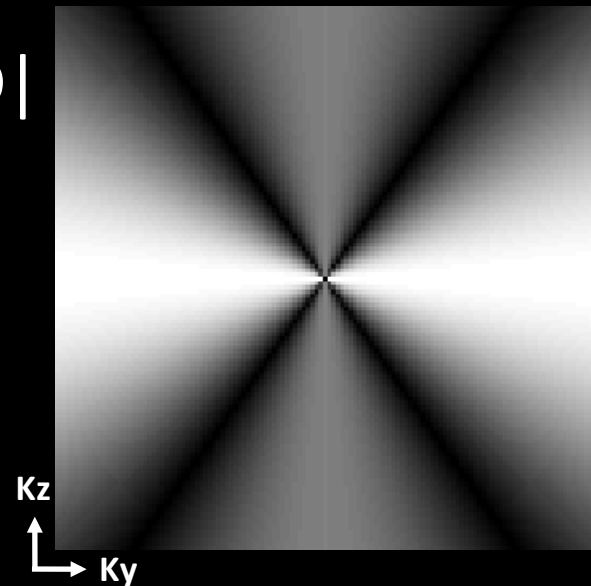
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- Estimation of the susceptibility map χ from the unwrapped phase φ involves solving an inverse problem,

$$\delta = \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \chi$$

- The inversion is made difficult by zeros in susceptibility kernel \mathbf{D}

$$\mathbf{D} = \frac{1}{3} - \frac{k_z^2}{k_x^2 + k_y^2 + k_z^2}$$

$|\mathbf{D}|$

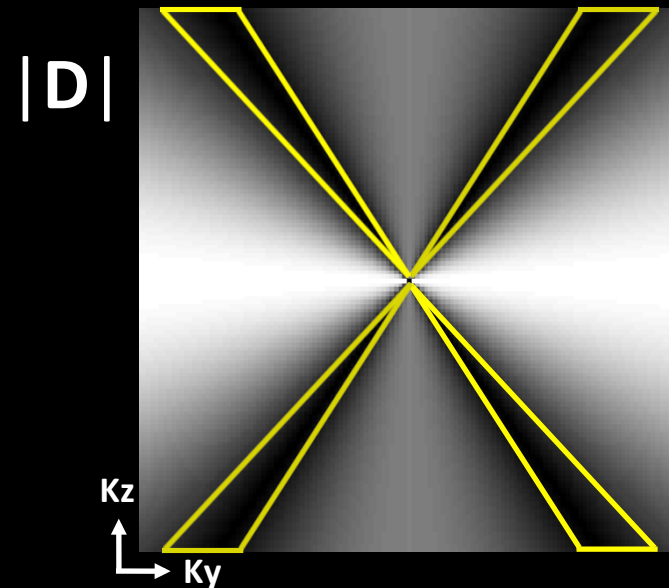


Quantitative Susceptibility Mapping (QSM)

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$$\delta = \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \chi$$

- The inversion is made difficult by zeros in susceptibility kernel \mathbf{D}
- Undersampling is due to physics
Not in our control



Regularized Susceptibility Inversion

- Use prior knowledge to estimate susceptibility map in the presence of undersampling
- **Prior:** Susceptibility is tied to the magnetic properties of the underlying tissue; hence it should vary smoothly within anatomical boundaries.
- Employ regularization that encourages smoothness within tissues, but avoids smoothing across boundaries.

L2 Regularized Susceptibility Inversion

- We solve for the susceptibility distribution with a convex program,

$$\min \underbrace{\left\| \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \chi - \delta \right\|_2^2}_{\text{Data consistency}} + \lambda \cdot \underbrace{\left\| \mathbf{M} \mathbf{G} \chi \right\|_2^2}_{\text{Regularizer}}$$

L2 Regularized Susceptibility Inversion

- We solve for the susceptibility distribution with a convex program,

$$\min \left\| \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \chi - \delta \right\|_2^2 + \lambda \cdot \left\| \mathbf{M} \mathbf{G} \chi \right\|_2^2$$

\mathbf{G} : Spatial gradient operator in 3D

\mathbf{M} : Binary mask derived from magnitude image, prevents smoothing across edges

λ : Determines the amount of smoothness

L2 Regularized Susceptibility Inversion

- We solve for the susceptibility distribution with a convex program,

$$\min \left\| \mathbf{F}^{-1} \mathbf{D} \mathbf{F} \chi - \delta \right\|_2^2 + \lambda \cdot \left\| \mathbf{M} \mathbf{G} \chi \right\|_2^2$$

Optimizer given by the solution of:

$$(\mathbf{F}^{-1} \mathbf{D}^2 \mathbf{F} + \lambda \cdot \mathbf{G}^T \mathbf{M} \mathbf{G}) \chi = \mathbf{F}^{-1} \mathbf{D}^T \mathbf{F} \delta$$

**Large linear system, solve rapidly with
Preconditioned Conjugate Gradient¹**

Wave-CAIPI accelerated QSM

- Susceptibility mapping relies on phase signal from a 3D Gradient Echo (GRE) acquisition
- Long echo times ($TE \approx 30\text{ms}$) are required for phase evolution to improve SNR
- This constraint on repetition time (TR) further increases QSM data acquisition time:

Whole-brain 3D GRE at 1mm^3 resolution:

240x240x120 FOV
TR = 40 ms } $T_{\text{acq}} = 19 \text{ min if fully-sampled}$

Wave-CAIPI allows rapid QSM acquisition:

$T_{\text{acq}} = 2.3 \text{ min at } R=3 \times 3$

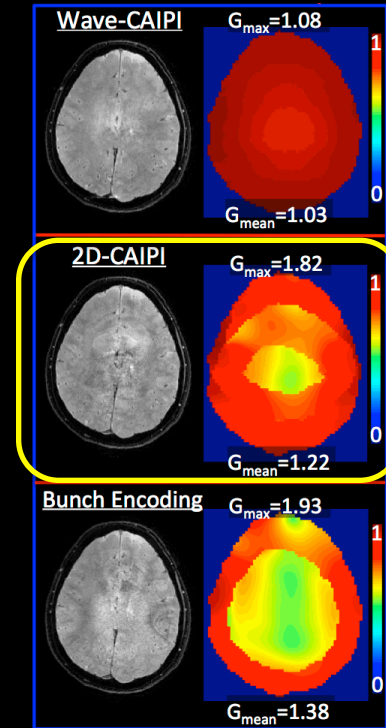
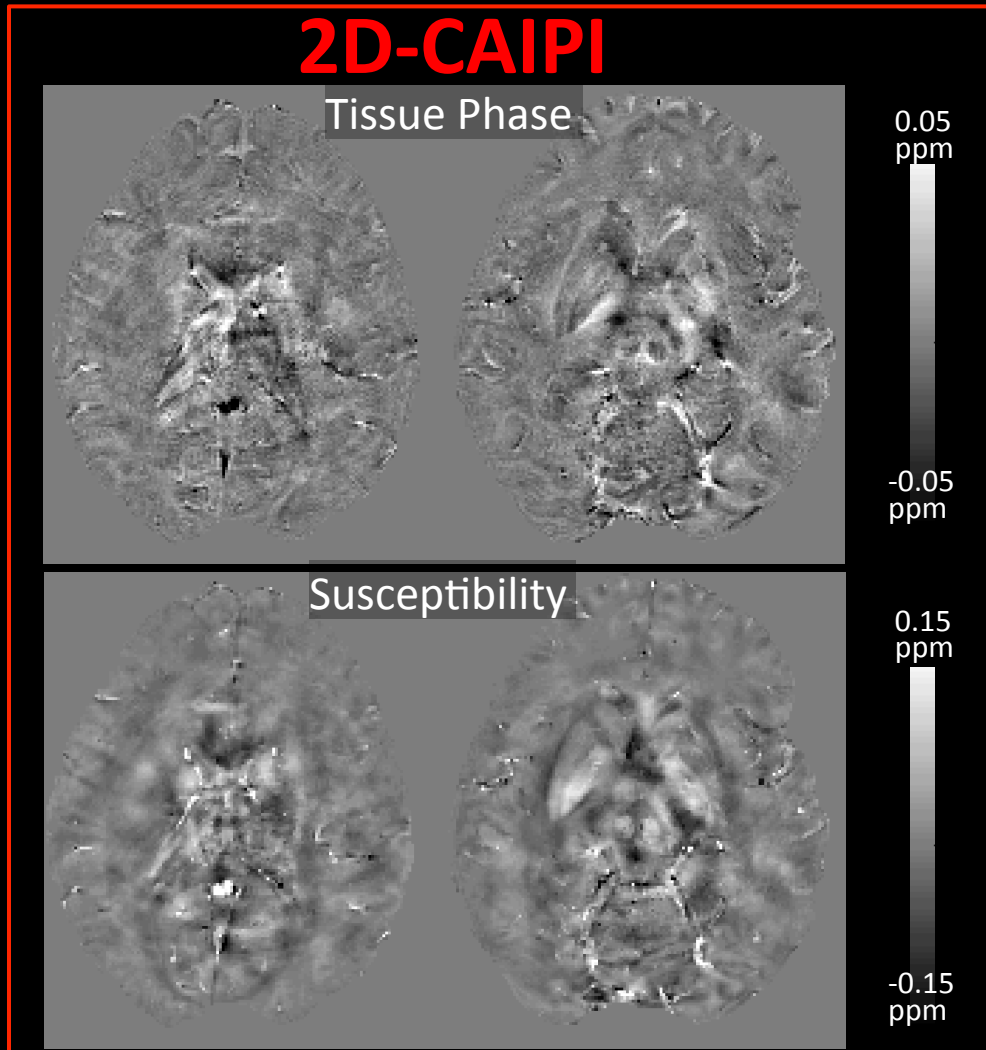
Wave-CAIPI accelerated QSM

- Compare in vivo phase and QSM from Wave-CAIPI, 2D-CAIPI and Bunch Phase Encoding:
 - At 3T and 7T
 - R = 3x3 acceleration, scan time = 2.3 min
 - 1 mm isotropic resolution
- Phase Processing:
 - Laplacian unwrapping¹ and
 - SHARP filtering for background removal²

} **14 seconds**
- Susceptibility Inversion:
 - Fast L2-regularized inversion³

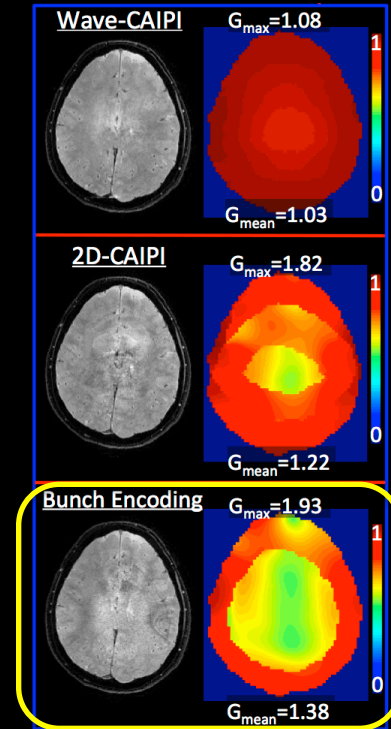
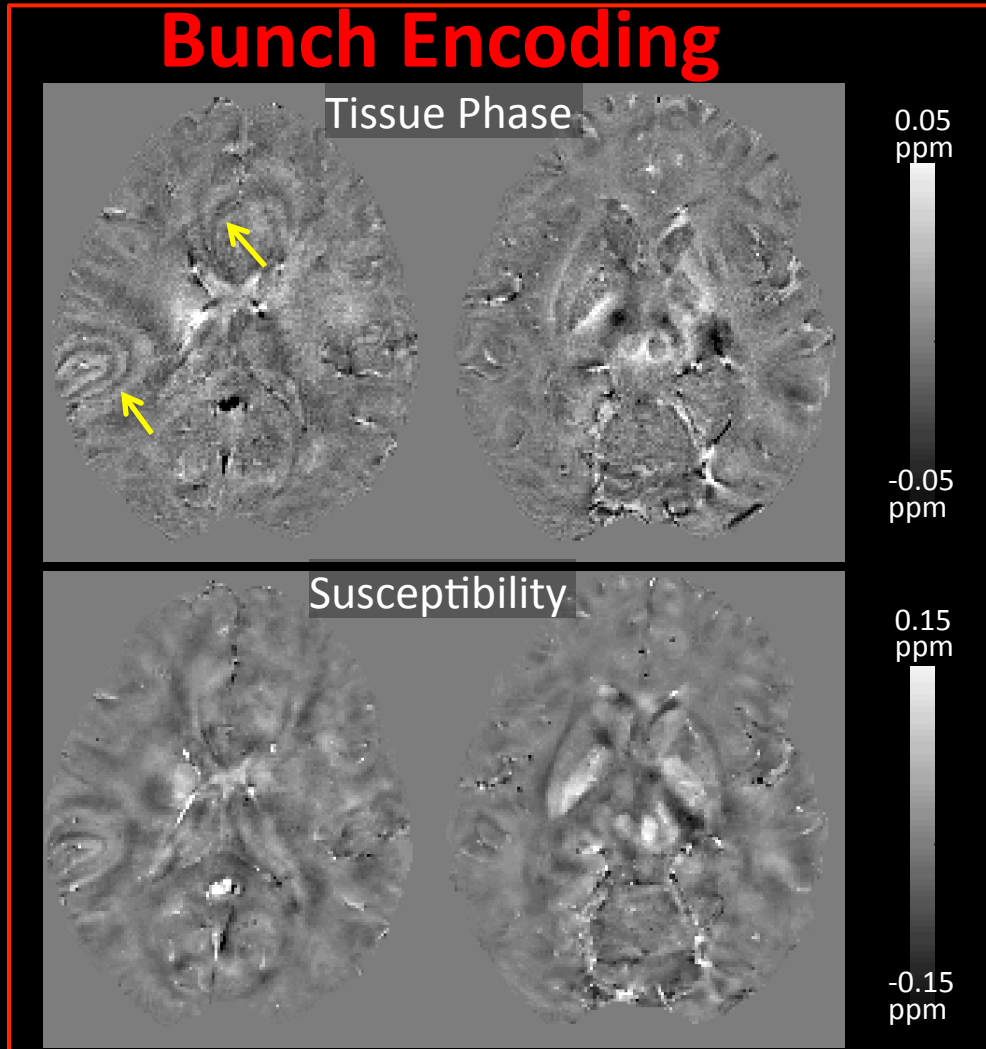
} **32 seconds**

3 Tesla, R=3x3, 1 mm iso, 2.3 min acq



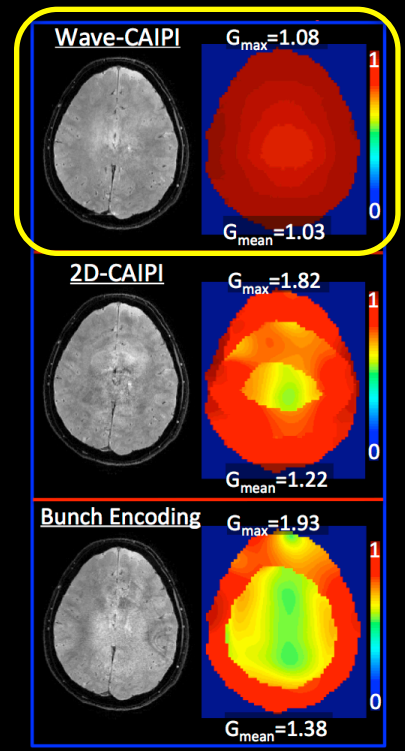
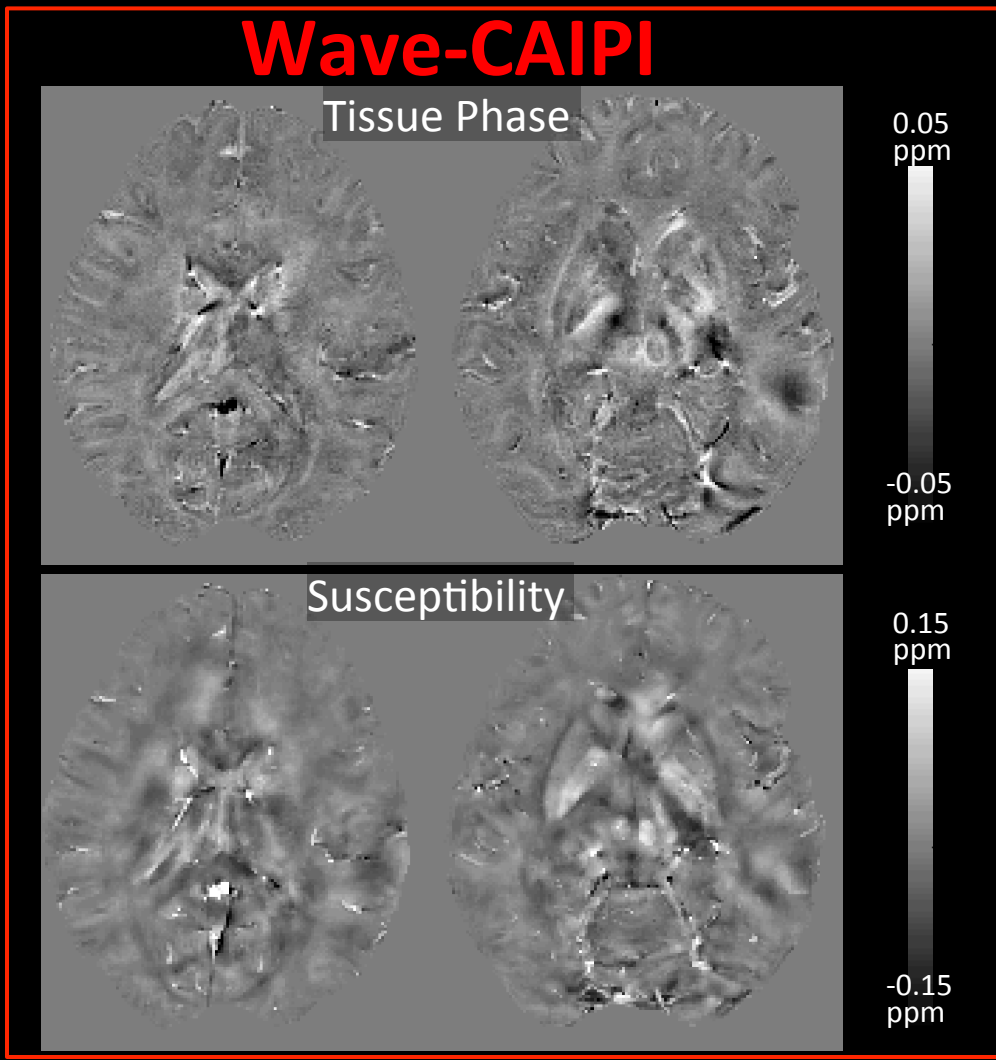
3 Tesla, R=3x3, 1 mm iso, 2.3 min acq

Bunch Encoding

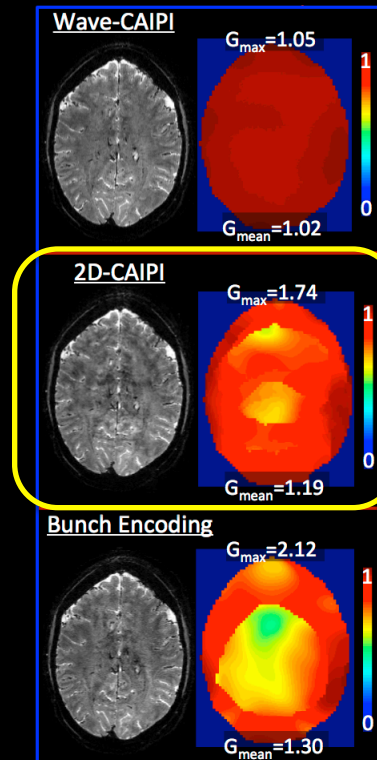
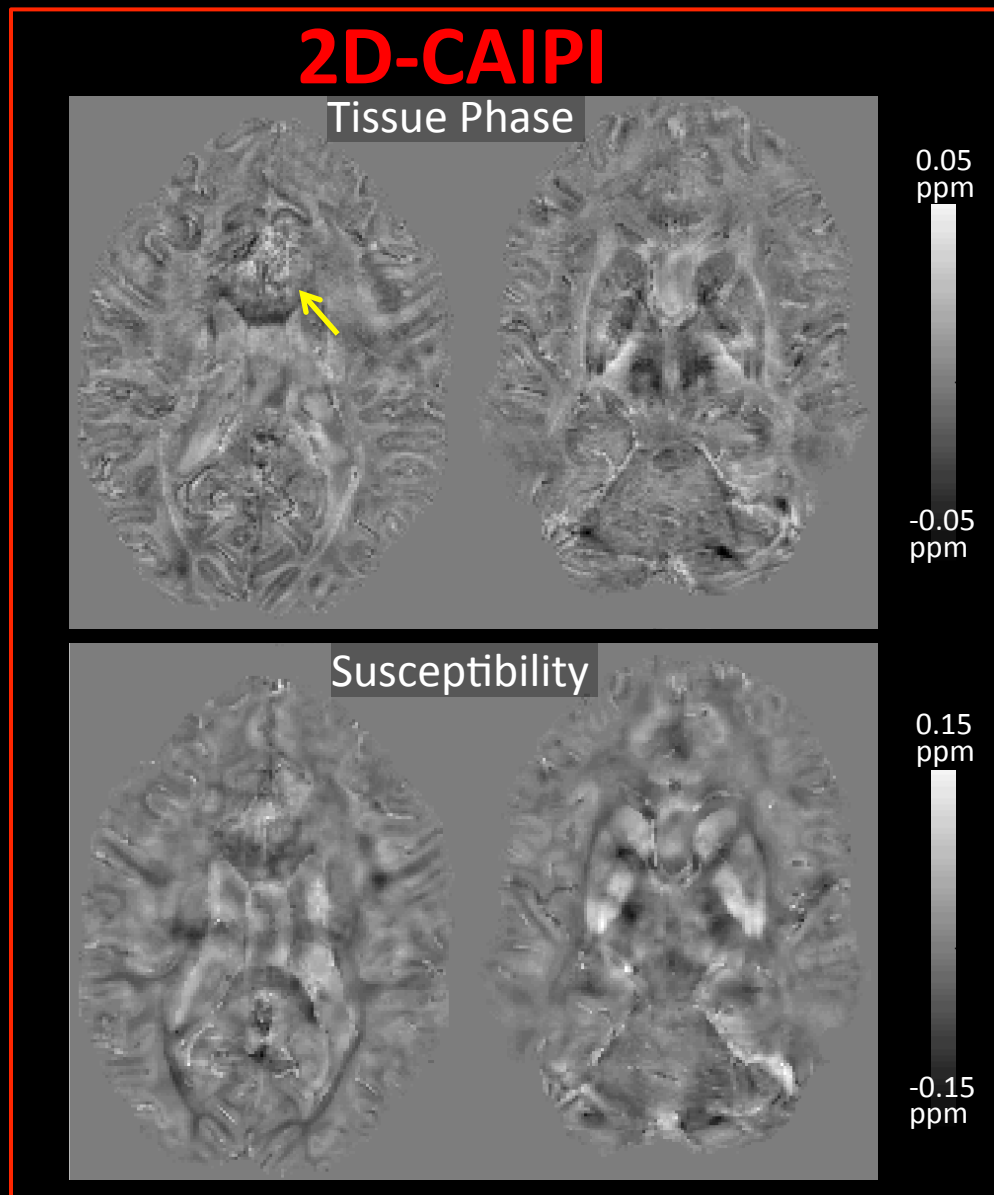


3 Tesla, R=3x3, 1 mm iso, 2.3 min acq

Wave-CAIPI



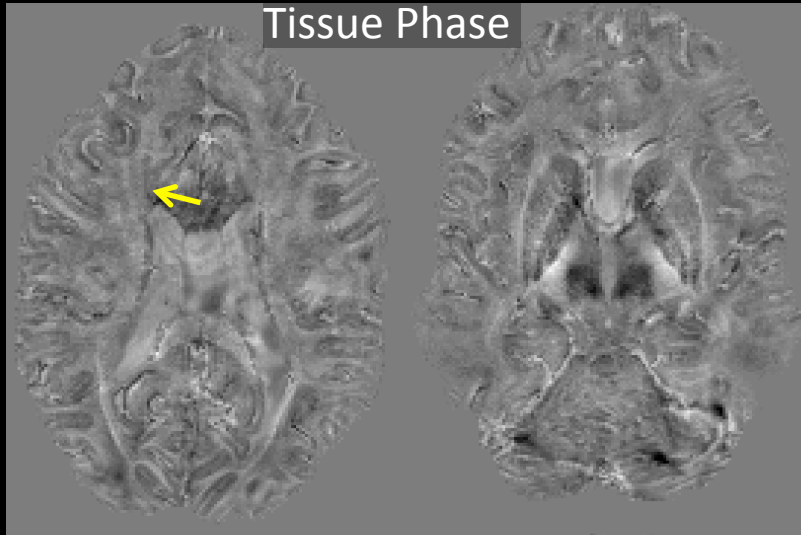
7 Tesla, R=3x3, 1 mm iso, 2.3 min acq



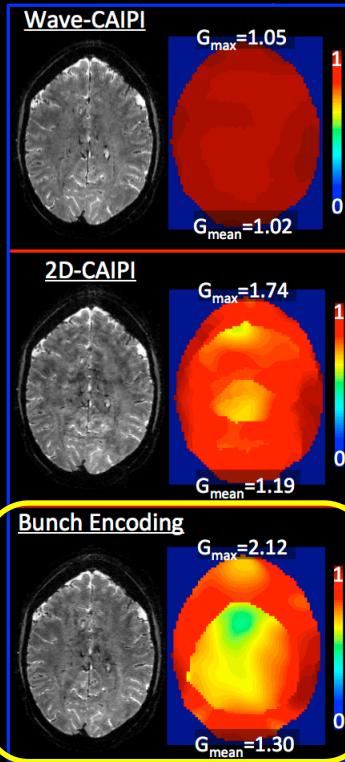
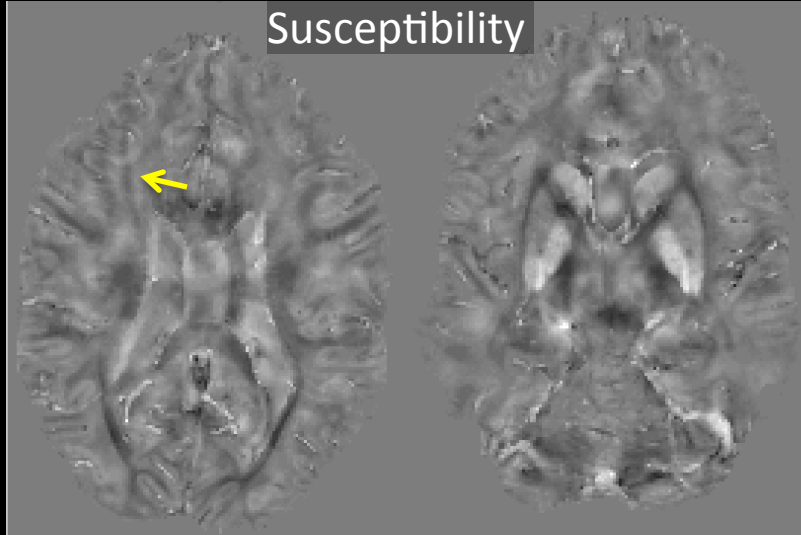
7 Tesla, R=3x3, 1 mm iso, 2.3 min acq

Bunch Phase

Tissue Phase



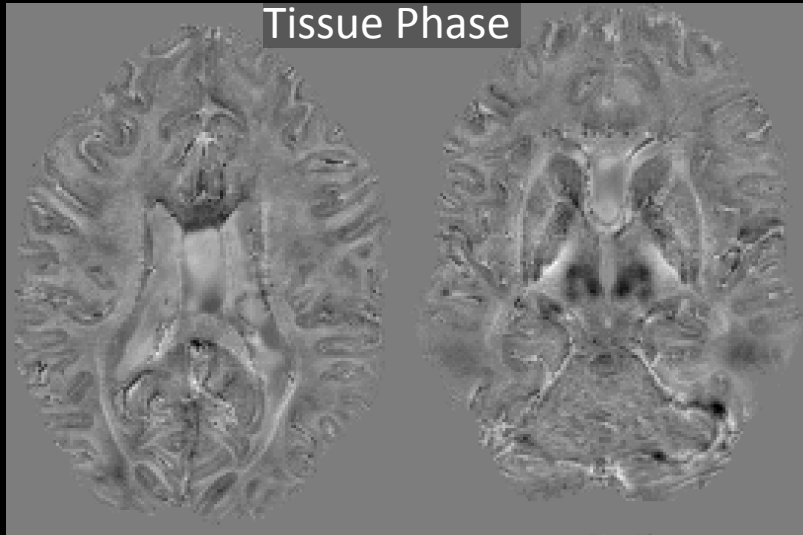
Susceptibility



7 Tesla, R=3x3, 1 mm iso, 2.3 min acq

Wave-CAIPI

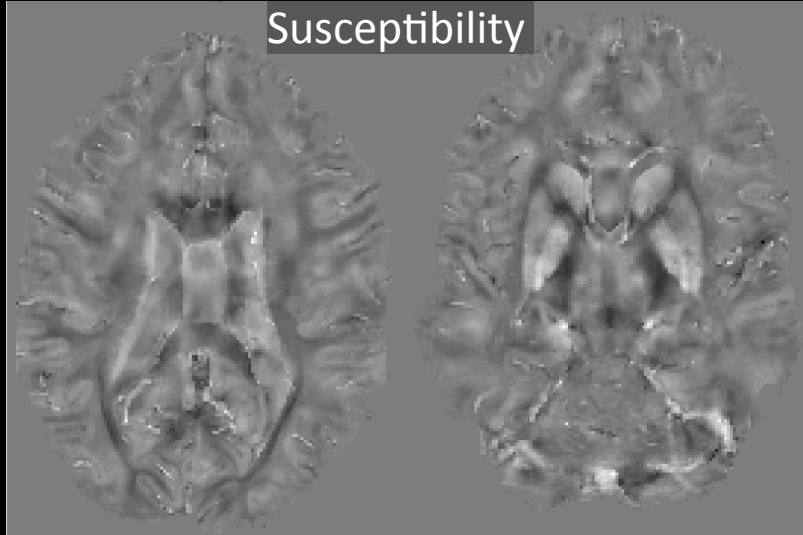
Tissue Phase



0.05
ppm

-0.05
ppm

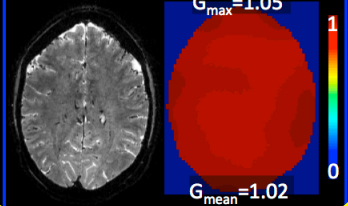
Susceptibility



0.15
ppm

-0.15
ppm

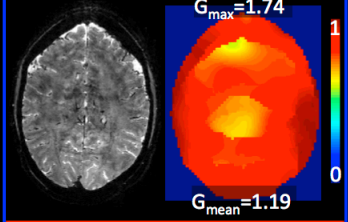
Wave-CAIPI



$G_{max}=1.05$

$G_{mean}=1.02$

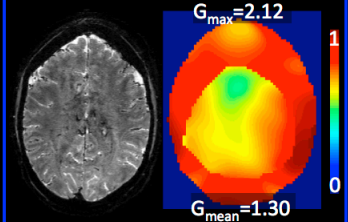
2D-CAIPI



$G_{max}=1.74$

$G_{mean}=1.19$

Bunch Encoding



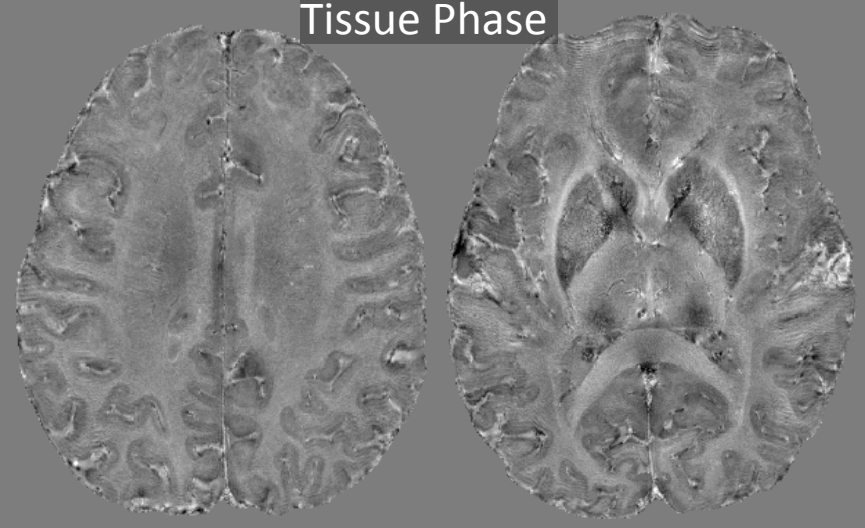
$G_{max}=2.12$

$G_{mean}=1.30$

7 Tesla, R=3x3, 0.5 mm iso, 5.1 min acq

Wave-CAIPI

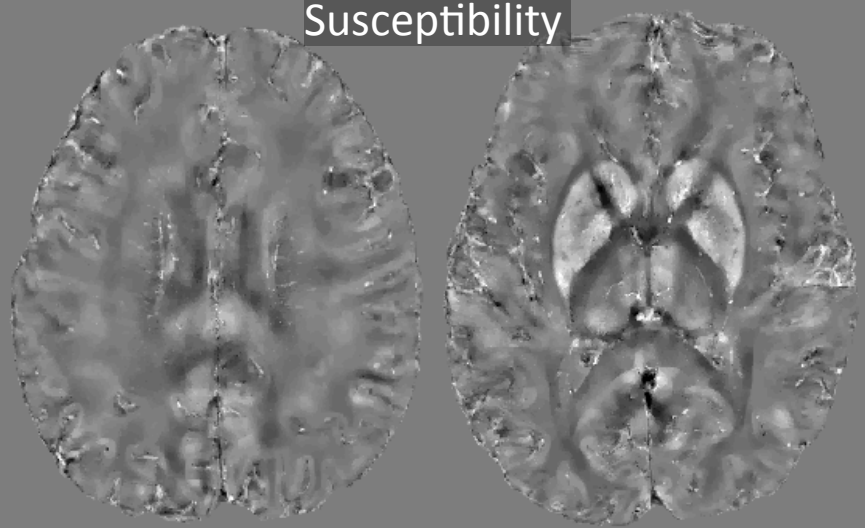
Tissue Phase



0.05 ppm

-0.05 ppm

Susceptibility



0.15 ppm

-0.15 ppm

Summary

- Propose Wave-CAIPI acquisition/reconstruction scheme for highly accelerated 3D imaging
- Wave-CAIPI offers 2-fold improvement in g-factor and image artifact penalties compared to 2D-CAIPI and Bunch Phase Encoding

Summary

- Propose Wave-CAIPI acquisition/reconstruction scheme for highly accelerated 3D imaging
- Wave-CAIPI offers 2-fold improvement in g-factor and image artifact penalties compared to 2D-CAIPI and Bunch Phase Encoding
- Deployed in GRE imaging, Wave-CAIPI allows 9-fold acceleration with \sim perfect SNR retention at 3T and 7T
- Combined with fast phase and susceptibility processing methods, it enables QSM at 1 mm resolution in 2.3 min

Thank you for your attention